

Delamination of a Composite Laminated under Monotonic Loading

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Abstract. Our work aims to analyze using the finite element method the evolution of the stress intensity factor (SIF) parameter K of three laminated folded plates stacks $[+\alpha, -\alpha]$, made of the same epoxy matrix and different reinforcement fibers (boron, graphite and glass). Our results show that the angle of orientation of the boron / epoxy composite has no great influence on the variation of the parameter K_I . Compared to composite graphite / epoxy and glass / epoxy, the laminated composite boron / epoxy reduces more the SIF K_I in the middle of the plate for angles $0^\circ \leq \alpha \leq 30^\circ$.

Keywords: Cracks, delamination, stress intensity factor, fibers orientations, finite element method and laminates.

1. Introduction

The use of long-fiber laminates and organic matrix (O.M.C) continues to grow in most of various fields of engineering applications. The good specific mechanical properties of these materials make it possible to relief structures, particularly in the aeronautical and aerospace industries. Although these materials have several advantages, they should be used with caution.

Damage mechanisms involved in laminated composites are contrary to that of conventional metallic materials. One of the most important types of deterioration encountered in laminated composite materials is the decomposition of the two layers. This damage is known as delamination, which can be observed according to the scale of study. The resistance of the material decreases significantly due to delamination.

Practically, it is very important to identify the initiation of delamination and prevent further spread resulting in ultimate failure [01]. In addition, the prediction for the beginning of the delamination is also useful for the structure design. Short et al. [02] have studied the effect of the geometry and location of a single square delamination. The results of their experiments and finite element analyzes show that the

size of the delamination and position through the thickness, affects the compression breaking load. Kutlu and Chang. [03] reported the first studies on the effects of delamination on the compression behavior of multiple laminates (one or two). They performed an analytical and experimental analysis to determine the effects of the size and position across the width of delamination. Wang et al. [04] studied the effects of single and multiple position delamination on compressive resistance of the composite reinforced with glass fiber. Their experimental and numerical results show that several delaminations reduce the compressive resistance more than one delamination. Li et al. [05] used a LayerWise method to study the effects of the size and position of several delamination for unidirectional and diagonal beams. Suemasu et al. [06] determines the behavior in compression and composite failure mechanism with several circular delaminations using cohesive interface elements. Their results indicate that the load capacity of a composite structure with several delaminations depends on the growth of delamination. Jayatilake et al. [07] have developed a 3D finite element model to study the dynamic behavior (free vibration) of multilayer composite sandwich panels with delaminated interlayer. The results suggest that the size of delamination and the boundary conditions are the main factors responsible for the reduction in stiffness due to damage in composite laminates. A survey was Conducted again by TODO et al. using the model and fashion II ENF (End Notched Flexure)

composite glass-fiber / vinyl ester [09]. Haneef et al. [08] have carried out finite element analysis to analyze the delamination effect on composite structures with two models. TODO and JAR presented a finite element study on micro-macro mechanical growth of interlaminar crack array fiberglass / epoxy DCB specimens for mode I [09]. Lonquan Liu et al. [10] studied the mechanical behavior of curved laminates experimentally and numerically using three right angle composite angles to determine progressive failure modes based on the Ye criterion of resistance failure. They found that the mode of failure of all specimens is delamination. Yang Liu and Dong W. Shu. [11] developed an analytical model to study the effect of a crack of the edge on the characteristics of vibration of the delaminated beams.

The present work aim is to analysis, by the finite element method, the evolution of the stress intensity factor parameter K of three laminated folded plates stacks [+ α , - α], made of the same epoxy matrix and various reinforcing fibers (boron, graphite and glass), by varying several parameters such as the fiber orientation, the delamination length and the load applied.

2. Geometric model

Our model is an orthotropic square plate of 150x20 mm² consisting of eight 0.125 mm thick crossed plies [+ α - α]; each layer with an epoxy matrix is reinforced by glass or graphite or bore fibers Fig.1.

The material mechanical properties of the unidirectional composites are shown in Table1 [12].

Table 1 Mechanical properties of composites

Proprieties	Glass/epoxy	Boron/epoxy	Graphite/epoxy
E11[MPa]	50000	208000	13400
E22[MPa]	14500	25400	10300
E33[MPa]	14500	25400	10300
ν_{12}	0.33	0.1677	0.33
ν_{13}	0.33	0.1677	0.33
ν_{23}	0.33	0.035	0.53
G ₁₂ [MPa]	2560	7200	5500
G ₁₃ [MPa]	2560	7200	5500
G ₂₃ [MPa]	2240	4900	3200

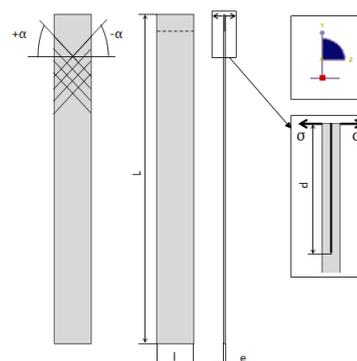


Fig. 1 Geometric model.

- l: width of the plate = 20 mm
- L: Length of the laminate sheet = 150 mm
- e: plate thickness = 1 mm (8 plies)
- d: Length of variable delamination (30 to 60) mm
- α : fiber orientation angle (+ α - α)
- σ : variable applied stress (1 to 10) MPa

The Simulation of linear tensile behavior and the influence of fiber orientation and other parameters, have been carried out using the numerical code Abaqus [13] and this for the analysis of composite structures was done by the finite element method. This code provides a complete system, incorporating not only the actual computing functions, but also the model construction functions (preprocessor) and output treatment (post-processor). To properly conduct this study, we have chosen a three-dimensional element whose quadrilateral elements are of quadratic type (see Fig. 2).

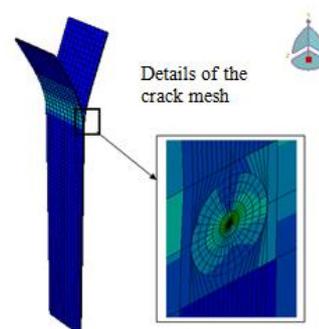
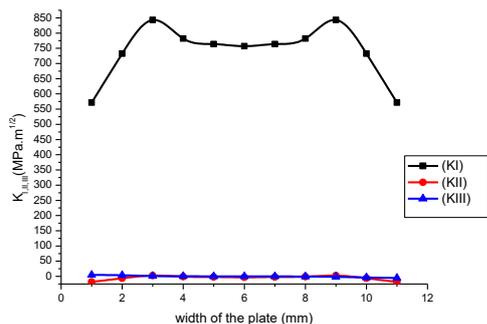


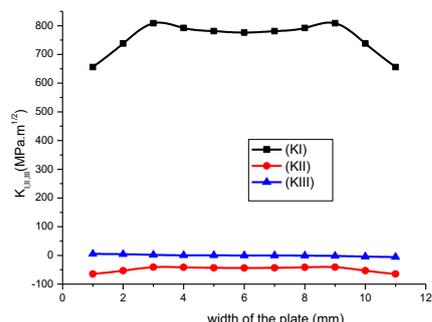
Fig. 2 Mesh with quadrilateral elements of quadratic type

3. results

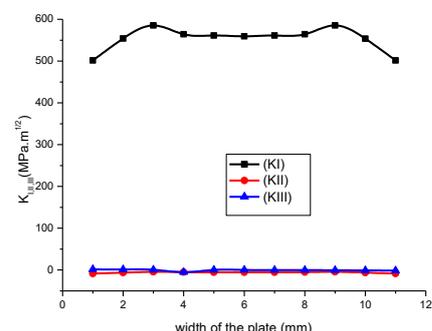
3.1 Influence of the width of delamination on stress intensity factors of three composite:



(a) glass/epoxy



(b) boron/epoxy



(c) graphite/epoxy

Fig. 4 Variation of the stress intensity factors K_I , K_{II} and K_{III} depending on the width of delamination of the three composites for $\alpha = 0^\circ$ and $d = 30\text{mm}$.

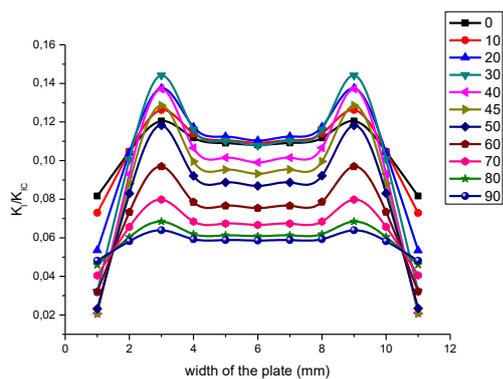
Figure 4 shows the variation of the stress intensity factors K_I , K_{II} and K_{III} depending on the width of delamination of glass / epoxy composite. It is noted that the delamination spread of the composite plate is carried out in pure mode I and this according to the force applied to the composite. K_I stress intensity factor is much higher than the other two failure modes according to the plan and the anti-slip map, which shows that the detachment of the folds happens in pure mode I. In our study the pure mode I is predominant and it is the only parameter to be considered and the two sliding modes K_{II} and K_{III} are neglected.

3.2 Influence of the width of delamination of the composite glass / epoxy on the K_I / K_{IC} ratio for different angles α ($+\alpha / -\alpha$) and different lengths "d"

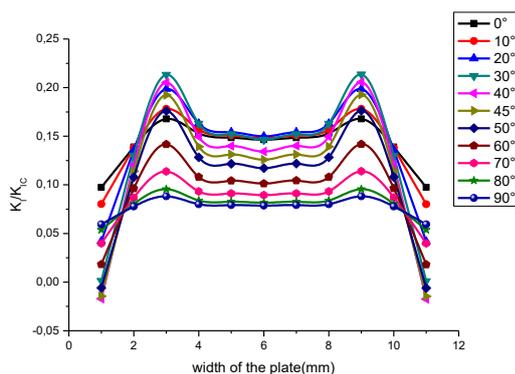
Figure 5 shows the variation of ratio K_I / K_{IC} ratio as a function of the delamination width for different angles of orientation $+\alpha/-\alpha$ of the folds of the glass / epoxy composite and different lengths d of the detached surface. The graphs of Figs. 5a, 5b, 5c, 5d, 5e, 5f and 5g are respectively determined for the delamination lengths 30 mm, 35 mm, 40 mm, 45 mm, 50 mm, 55 mm and 60 mm. It should be noted that regardless of the length of detachment of the layers of the glass / epoxy laminate composite, the curve of the ratio K_I / K_{IC} has a symmetry with respect to the middle of the delamination width and therefore the analysis could be performed over half the width of delamination. From the numerical results obtained by the finite element method, there are three different zones of the curve of the ratio K_I / K_{IC} :

The first zone is located at the free edges of the composite plate over a distance of 10% of the delamination half width in which the value of K_I / K_{IC} ratio depends on the angle α of the layers of the laminated composite and the surface of detachment and it reaches minimum values in this area and even negative values. At the free edges of the composite, it can be seen that regardless of the angle α and the length d of the detachment surface, the propagation of the delamination is either slowed down or completely stopped.

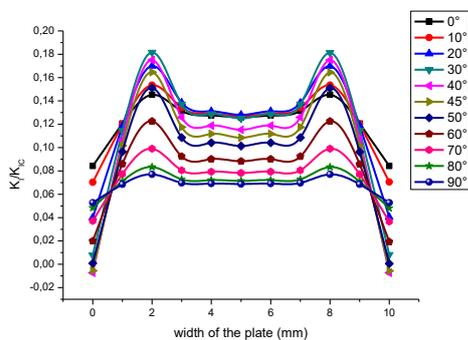
The second zone is in the vicinity close to the free ends over a distance of 20% of the half width of the detachment. It is noted that regardless of the angle α and the length L the curve of the ratio K_I / K_{IC} is in the form of a parabola, it increases progressively to reach a peak and then decreases to a stable value in the middle of the plate composite. It is noted that the peak of the stress intensity factor is more intense for the angles of orientations of the fibers ranging from 0° to 50° and its intensity decreases with the increase of the angle α in the interval $[60^\circ, 90^\circ]$. The two orientations of the fibers at the 80° and 90° angles result in a small peak of the SIF K_I . It is also observed that the increase in the detachment surface leads to an increase in the peak of the SIF K_I .



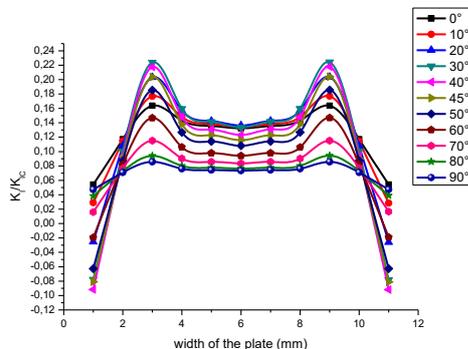
(a) Delamination lengths 30mm



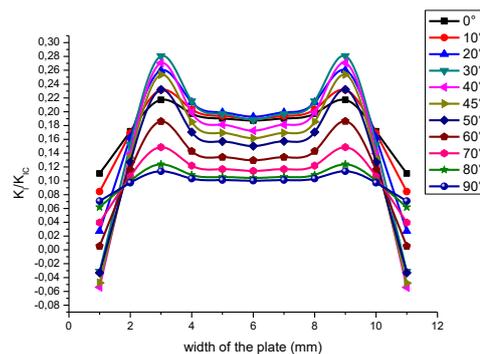
(b) Delamination lengths 35mm



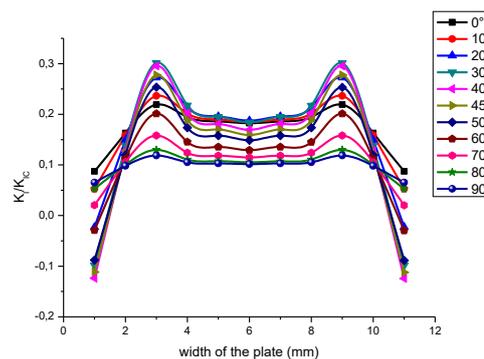
(c) Delamination lengths 40mm



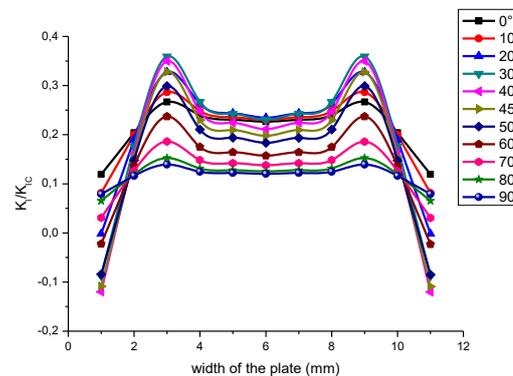
(d) Delamination lengths 45mm



(e) Delamination lengths 50mm



(f) Delamination lengths 55mm



(g) Delamination lengths 60mm

Fig. 5 Variation of K_I / K_{IC} depending on the width of delamination of the composite glass / epoxy for different angles α ($+\alpha / -\alpha$) and different lengths (a: 30 mm b: 35 mm c: 40 mm, d: 45mm, e 50mm f: g 55mm and 60mm).

The third zone is in the middle of the composite plate over a distance of 20% of the half width of delamination. It can be seen that, regardless of the angle α and the length L , the K_I / K_{IC} ratio is almost constant and the level of the stress intensity factor K_I depends strongly on the angle of orientation of the fibers and the length of delamination.

3.3 Influence of fiber orientation on the K_I / K_{IC} ratio in the middle of the plate

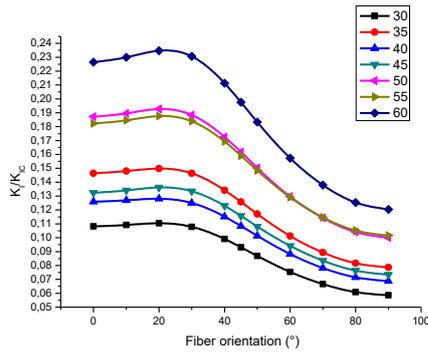


Fig. 6 variation of the K_I / K_{IC} ratio in the middle of the composite plate as a function of the angle α for different lengths L of the detachment surface.

Figure 6 illustrates the variation of the K_I / K_{IC} ratio in the middle of the composite plate as a function of the angle α for different lengths d of the detachment surface. It should be noted that whatever the length d , the ratio K_I / K_{IC} is almost constant for angles α ranging from 0° to 30° and then decreases proportionally to the angle of orientation of the folds to a minimum value corresponding to $\alpha = 90^\circ$.

3.4 Influence of fiber orientation on the K_I / K_{IC} ratio at the free edge of the plate

Figure 7 illustrates the variation of the K_I / K_{IC} ratio at the free edge of the composite plate as a function of the angle α for different lengths d of the detachment surface. It can be seen that the curve of the parameter K_I / K_{IC} is in the form of a parabola whose extremum corresponds to the angle $\alpha = 40^\circ$ for the different lengths of delamination. It is also noted that the variation of K_I / K_{IC} is not proportional to the detachment surface, confirming the results obtained previously (see Figure 6).

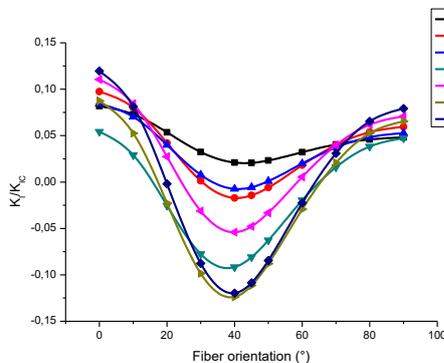


Fig. 7 Variation of the K_I / K_{IC} ratio to the free edge

of the composite plate as a function of the angle α of the glass / epoxy for different lengths d of the detachment surface.

3.5 Influence the length of delamination on factor K_I

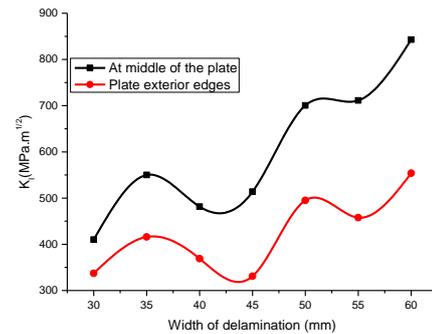
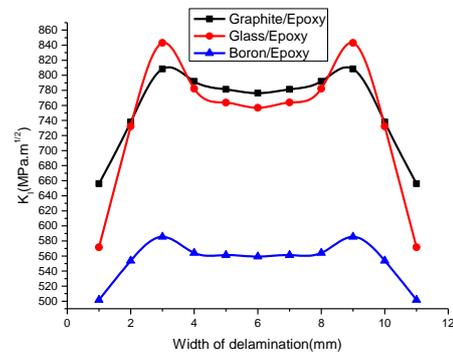


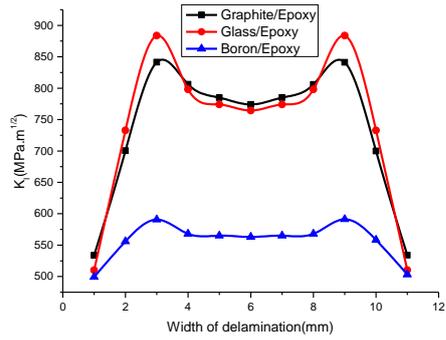
Fig. 8 Variation of the FIC K_I as a function of the delamination length for different positions (middle and outer) with $\alpha = 90^\circ$.

Figure 8 shows the variation of the SIF K_I as a function of the delamination length for an angle $\alpha = 90^\circ$, this curve shows the effect of the length of the detachment surface on the parameter K_I . From the results obtained numerically, it is noted on one hand that the parameter K_I increases with the increase of delamination the length and on the other hand this variation is not proportional to this length.

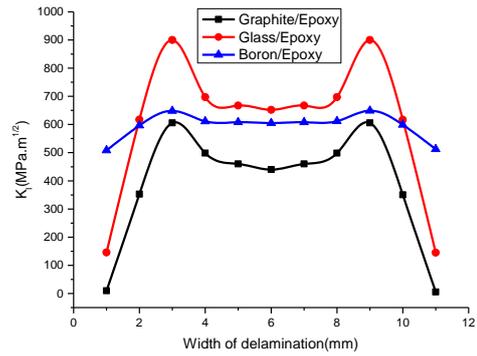
3.6 Influence of the mechanical properties of the composite on the parameter K_I



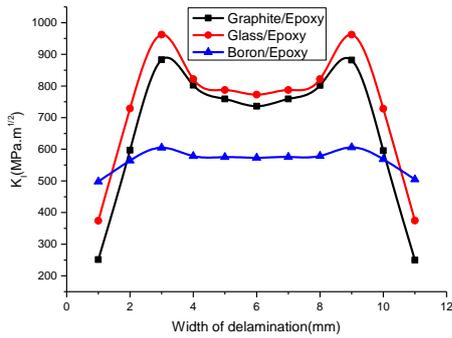
(a) Fiber orientation 0°



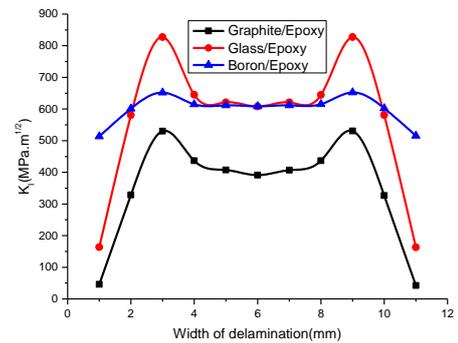
(b) Fiber orientation 10°



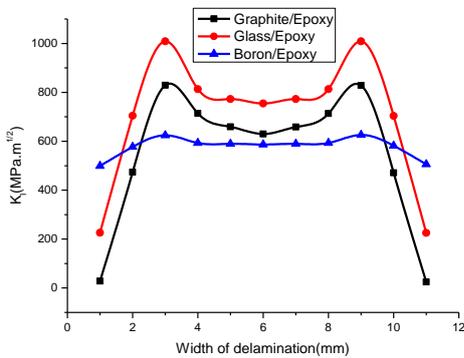
(f) Fiber orientation 45°



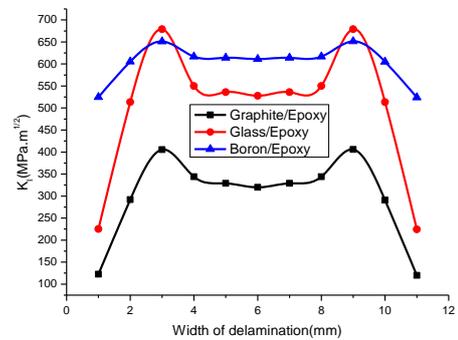
(c) Fiber orientation 20°



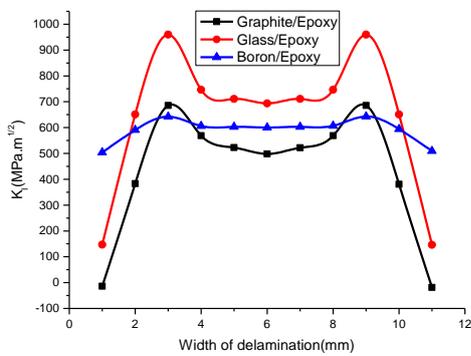
(g) Fiber orientation 50°



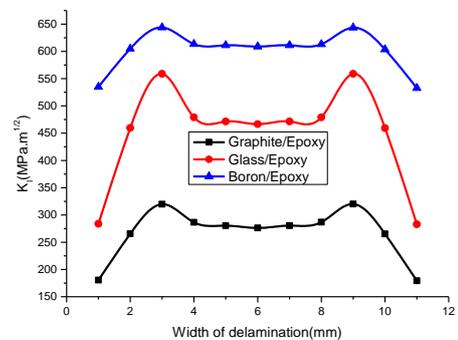
(d) Fiber orientation 30°



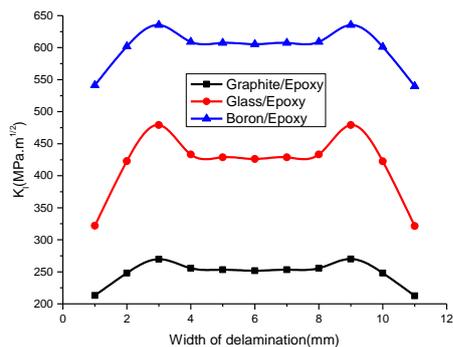
(h) Fiber orientation 60°



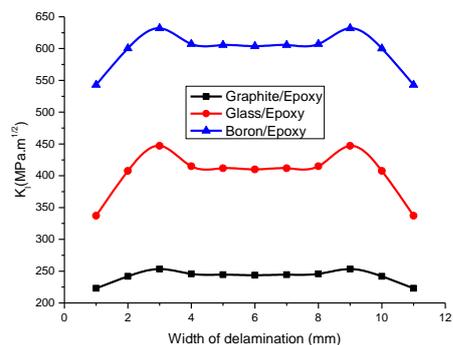
(e) Fiber orientation 40°



(i) Fiber orientation 70°



(j) Fiber orientation 80°



(k) Fiber orientation 90°

Fig. 9 Variation of the K_I factor as a function of the width of delamination of composites (glass/epoxy, graphite/epoxy and boron/epoxy) for different angles $\alpha(+\alpha/-\alpha)$ (has a: 0°, b: 10°, c: 20°, d: 30°, e: 40°, f: 45°, g: 50°, h: 60°, i: 70°, j: 80° and k: 90°).

Figure 9 illustrates the variation of the SIF K_I as a function of the delamination width for the three glass / epoxy, graphite / epoxy and boron / epoxy laminated composites. These graphs are determined for a detachment length equal to 30 mm and the angles of orientations of the folds ranging from 0° to 90° with a pitch of 10° and they show the influence of the mechanical properties of the composite on the parameter K_I . It is noted that the SIF K_I is almost constant along the delamination width of the composite plate with the presence of a slight variation at the free ends of the boron / epoxy composite, whatever the angle α of the fibers. Consequently, for this type of composite, the angle of orientation of the fibers does not have a great influence on the variation of the parameter K_I . Compared to graphite / epoxy and glass / epoxy composites, the boron / epoxy laminate composite further reduces the SIF K_I in the middle of the plate for angles $0^\circ \leq \alpha \leq 30^\circ$. However, for

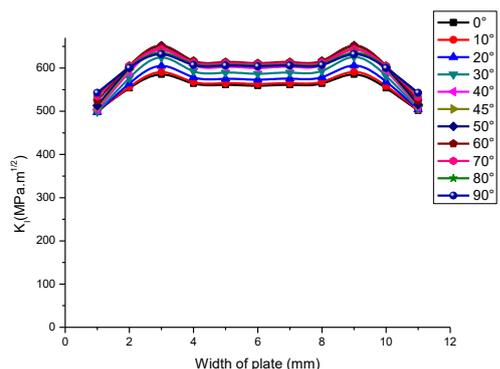
angles $40^\circ \leq \alpha \leq 60^\circ$ the boron / epoxy composite loses its resistance qualities with respect to the other two graphite / epoxy and glass / epoxy composites. It is noted that the properties of these latter composites allow a better attenuation of the parameter K_I compared to the boron / epoxy composite for angles of orientation of the fibers greater than 60°.

The results obtained numerically by the element method show the variation of the stress intensity factor as a function of the width of the delamination for two angles of orientation of the plies of the graphite / epoxy and glass / epoxy laminate composite ($\alpha = 0^\circ$ and $\alpha = 20^\circ$). It is noted that the two curves determined for these two angles are totally confounded, that is to say that the properties of these two composites have no influence on the propagation of delamination.

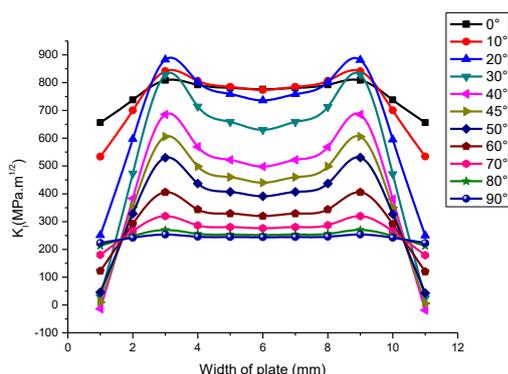
It is observed that for the two angles of orientation of the fibers $\alpha = 30^\circ$ and $\alpha = 40^\circ$, the stress intensity factor of the glass / epoxy composite is higher than that of the graphite / epoxy composite in the middle of the separation width and in the vicinity close to the free end of the composite plate but it remains constant at the free edges of the two composites. The difference in the stress intensity factors of glass / epoxy and graphite / epoxy composites increases with increasing fiber orientation angle $\alpha = 50^\circ$ and $\alpha = 60^\circ$ in the middle of the delamination width and in the vicinity close to the free ends, however the phenomenon is reversed at the free ends of the composites. For angles ranging from 70° to 90° the difference between the stress intensity factors of glass / epoxy and graphite / epoxy composites is almost constant over the entire delamination width whose level of the SIF K_I of the glass / Epoxy is always higher than that of the graphite / epoxy composite.

The mechanical properties of the graphite / epoxy composite increase the mechanical strength of the composite plate and improve its mechanical strength during operation, in particular for an angle of orientation of the folds equal to 90°.

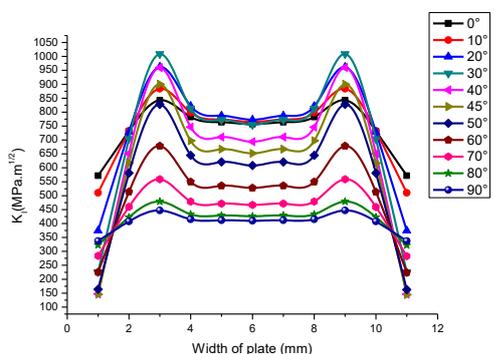
3.7 Influence of the delamination length on the K_I factor for different orientations of the fibers



(a) glass/epoxy



(b) boron/epoxy



(c) graphite/epoxy

Fig. 10 Variation of the K_I factor as a function of delamination with of the three composite and for various angles $\alpha(+\alpha/-\alpha)$ (a: boron/epoxy, b: glass/epoxy and c: graphite/epoxy.)

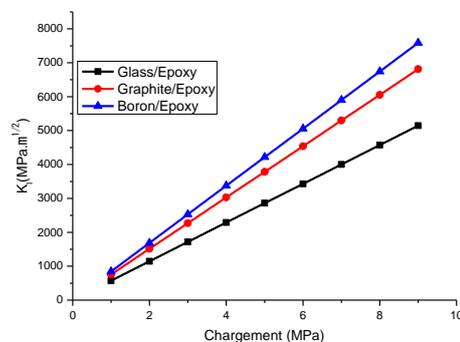
Figure 10a, 10b and 10c show the variation of the SIF K_I as a function of the width of the detachment of the three composites for different orientation angles of the fibers. These graphs confirm the result obtained in figure 9.

3.8 Influence of the applied load on the K_I factor for different orientations of the fibers

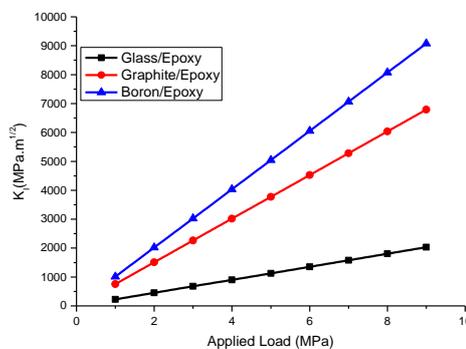
Figure 11a, 11b and 11c show the variation of the FIC K_I as a function of the force applied to the glass / epoxy composite plate for the three orientation angles of the respective fibers 0° , 30° and 90° . It can be seen that whatever the angle of the folds $+\alpha / -\alpha$ the SIF K_I increases with the increase of the applied load. When the fibers are oriented at an angle $\alpha = 0^\circ$, the maximum load leads to the damage of the composite in the vicinity close to the free ends.

On the other hand, the orientation of the folds at an angle $\alpha = 90^\circ$ leads to a significant reduction of the SIF K_I , which slows down the delamination propagation even when the composite is subjected to high intensity charges. The orientation of the folds at an angle $\alpha = 30^\circ$ of the glass / epoxy composite stressed at intense loads leads to a SIF K_I which exceeds the toughness of the composite material, which promotes delamination and weakens the mechanical strength of the laminated composite.

3.9 Influence of the applied load on the K_I factor for different materials



(a) Case $\alpha=0^\circ$



(b) Case $\alpha=30^\circ$

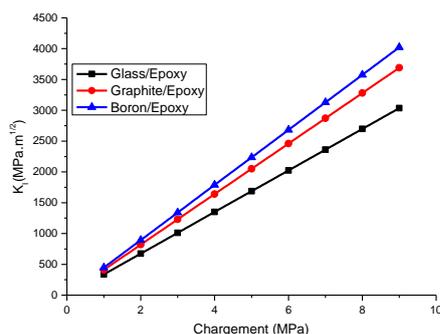
(b) Case $\alpha=90^\circ$

Fig. 12 Variation of the K_I factor as a function of the applied load of the three composites and for different angles α ($+\alpha / -\alpha$) (a: $\alpha = 0^\circ$, b: $\alpha = 30^\circ$ and c: $\alpha = 90^\circ$).

Figure 12 illustrates the variation of the SIF K_I as a function of the force applied to the glass / epoxy, graphite / epoxy and glass / epoxy composite plate for the three angles of orientation of the fibers respectively 0° , 30° and 90° . It is noted that the SIF varies in proportion to the load applied to the glass / epoxy composite. The curve of the stress intensity factor is a straight line.

4. Conclusions

This numerical analysis by the finite element methods allows us to draw the following conclusions:

- The propagation of pure mode I delamination depends on the type of stress applied to the laminated composite. In our study, mode I was decoupled of the two modes II and III.

- The delamination of the composite begins at the zone which is in the vicinity close to the two free ends of the laminated composite.

- The peak of the stress intensity factor is more intense for the angles of orientations of the fibers ranging from 0° to 50° and its intensity decreases with the increase of the angle α in the interval $[60^\circ, 90^\circ]$.

- The two orientations of the fibers at 80° and 90° angles result in a small peak of the SIF K_I .

- The increase of the detachment surface leads to an increase of the peak of the SIF K_I .

- Regardless of the angle α and the length d , the K_I / K_{IC} ratio is almost constant in the middle over a distance of 40% of the delamination width and the level of the stress intensity factor K_I strongly depends on the angle fiber orientation and delamination length. The parameter K_I reaches a minimum value for an

angle of the fibers $\alpha = 90^\circ$.

At the free edges of the composite plate, the K_I / K_{IC} ratio depends on the angle α of the layers of the laminated composite and the detachment surface and reaches minimum values in this area and even negative values. At the free edges of the composite, it can be seen that whatever the angle α and the length d of the detachment surface. Therefore the propagation of the delamination is either slowed down or totally stopped. The angle of the fibers equal to 40° leads to a decrease in the stress intensity factor and the variation of the parameter K_I is not proportional to the detachment length.

The mechanical properties of the graphite / epoxy composite increase the mechanical strength of the composite plate and improve its mechanical strength during operation, in particular for an angle of orientation of the folds equal to 90° . Compared with graphite / epoxy and glass / epoxy composites, the boron / epoxy laminate composite reduces more the SIF K_I in the middle of the plate for fiber angles $0^\circ \leq \alpha \leq 30^\circ$. However, for corners the boron / epoxy composite loses its qualities of resistance.

Whatever the angle of the folds $+\alpha / -\alpha$ the SIF K_I grows proportionally with the increase of the applied load.

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