and the phase. So even if the frequency is slightly changing, this estimate will guide us through the calculations. This is unlike TEO where you are not sure about the real values of the frequencies.

The presented stochastic calculus based approach could be extended to the case that both the amplitude and phase are randomly changing. This and other issues are currently under investigation.

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