

# Simulation of Absorption and Steady State Fluorescence Spectra, B- $\alpha$ /B- $\beta$ Ring from Photosynthetic Complex LH4

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**Abstract:** Photosynthesis starts with the absorption of a solar photon by one of the light-harvesting (LH) pigment-protein complexes and transferring excitation energy to the reaction center where charge separation is initiated. The geometric structure of some LH complexes is known in great detail, e.g. for LH2 and LH4 complexes of purple bacteria. Properties of such complexes are strongly influenced by their interactions with environment. These interactions could be modeled by static and dynamic disorder. Absorption and steady state fluorescence spectra of B- $\alpha$ /B- $\beta$  ring from LH4 complex within full Hamiltonian model are investigated in this contribution and compared with our previous results within the nearest neighbour approximation model. Different types of static disorder are considered and discussed. Comparison of the results for B- $\alpha$ /B- $\beta$  ring from LH4 complex and B850 ring from LH2 complex is also done.

**Key-Words:** LH4, LH2, absorption and fluorescence spectrum, static and dynamic disorder

## 1 Introduction

Photosynthesis is the process by which green plants and certain other organisms (bacteria, blue-green algae) transform light energy into chemical energy. During this process light energy is captured and used to convert water, carbon dioxide, and minerals into oxygen and energy-rich organic compounds. In chemical terms, photosynthesis is a light-energized oxidation–reduction process. Oxidation refers to the removal of electrons from a molecule; reduction refers to the gain of electrons by a molecule. These reactions occur in two stages: the light stage, consisting of photochemical (i.e., light-capturing) reactions; and the dark stage, comprising chemical reactions controlled by enzymes. During the first stage, the energy of light is absorbed and used to drive a series of electron transfers, resulting in the synthesis of ATP and the electron-donor reduced nicotine adenine dinucleotide phosphate (NADPH). During the dark stage, the ATP and NADPH formed in the light-capturing reactions are used to reduce carbon dioxide to organic carbon compounds [1].

Our interest is mainly focused on first (light) stage of photosynthesis in purple bacteria. Solar photons are absorbed by a complex system of membrane-associated pigment-proteins (light-harvesting (LH) antenna) and the electronic excited state is efficiently

transferred to a reaction center, where the light energy is converted into a chemical energy [2]. The antenna systems of photosynthetic units from purple bacteria are formed by ring units LH1, LH2, LH3, and LH4. The geometric structure is known in great detail from X-ray crystallography. The general organization of above mentioned light-harvesting complexes is the same: identical subunits are repeated cyclically in such a way that a ring-shaped structure is formed. However the symmetries of these rings are different.

Crystal structure of LH2 complex contained in purple bacterium *Rhodospseudomonas acidophila* was first described in high resolution by McDermott et al. [3], then further e.g. by Papiz et al. [4]. The bacteriochlorophyll (BChl) molecules are organized in two concentric rings. One ring features a group of nine well-separated BChl molecules (B800) with absorption band at about 800 nm. The other ring consists of eighteen closely packed BChl molecules (B850) absorbing around 850 nm. The whole LH2 complex is nonameric, it consists of nine identical subunits. LH2 complexes from other purple bacteria have analogous ring structure.

Some bacteria contain also other types of complexes such as the B800-820 LH3 complex (*Rhodospseudomonas acidophila* strain 7050) or LH4 complex (*Rhodospseudomonas palustris*). LH3 com-

plex like LH2 one is usually nonameric but LH4 one is octameric (it consists of eight identical subunits). While the B850 dipole moments in LH2 ring have tangential arrangement, in the LH4 main B- $\alpha$ /B- $\beta$  ring they are oriented more radially. In addition, mutual interactions of the nearest neighbour BChls in this LH4 ring are approximately two times smaller in comparison with B850 ring from LH2 complex and they have opposite sign. The other difference is the presence of two additional BChl rings in LH4 complex [5]. Different arrangements manifest themselves in different optical properties.

The intermolecular distances under 1 nm determine strong exciton couplings between corresponding pigments. That is why an extended Frenkel exciton states model could be used in theoretical approach. In spite of extensive investigation, the role of the protein moiety in governing the dynamics of the excited states has not been totally clear yet. At room temperature the solvent and protein environment fluctuates with characteristic time scales ranging from femtoseconds to nanoseconds. The simplest approach is to substitute fast fluctuations by dynamic disorder and slow fluctuations by static disorder.

Static disorder effect on the anisotropy of fluorescence for LH2 complexes was studied by Kumble and Hochstrasser [6] and Nagarajan et al. [7, 8]. We extended these investigations by consideration of dynamic disorder. We studied this effect for simple model systems [9–11] and then for models of B850 ring (from LH2) [12, 13]. Various types of uncorrelated static disorder (in local excitation energies, in transfer integrals, etc.) and correlated one (e.g., elliptical deformation) were used in the past [14–16] and also different arrangements of optical dipole moments were compared [17–20]. Recently we have focused on the modelling of absorption and steady state fluorescence spectra of LH2 and LH4 complexes within the nearest neighbour approximation model [21–25]. We have also extended our model to full Hamiltonian model and published the results for different types of static disorder [26–30]. Very recently we have started to explore full LH2 complex (B850 ring and B800 ring) [31].

Main goal of this paper is presentation of the steady state fluorescence and absorption spectra simulations for B- $\alpha$ /B- $\beta$  ring from LH4 complex within full Hamiltonian model with static disorder in radial positions of molecules on the ring. The results are discussed and compared with our previous ones within the nearest neighbour approximation model. Comparison of the results calculated as for LH4 complex as for LH2 one for different types of static disorder is also done.

The rest of the paper is structured as follows. Sec-

tion 2 introduces the ring model with static and dynamic disorder (interaction with phonon bath) and the cumulant expansion method, which is used for the calculation of spectral responses of the system with exciton-phonon coupling. Numerical considerations are mentioned in Section 3, used units and parameters could be found in Section 4. Results of our simulations are presented and discussed in Section 5 and some conclusions are drawn in Section 6.

## 2 Model

The Hamiltonian of an exciton in the ideal ring coupled to a bath of harmonic oscillators reads

$$H = H_{\text{ex}}^0 + H_s + H_{\text{ph}} + H_{\text{ex-ph}}. \quad (1)$$

First term,

$$H_{\text{ex}}^0 = \sum_{m,n=1(m \neq n)}^N \bar{J}_{mn} a_m^\dagger a_n, \quad (2)$$

corresponds to an exciton, e.g. the system without any disorder. The operator  $a_m^\dagger$  ( $a_m$ ) creates (annihilates) an exciton at site  $m$ ,  $\bar{J}_{mn}$  (for  $m \neq n$ ) is the so-called transfer integral between sites  $m$  and  $n$ .

Inside one ring the pure exciton Hamiltonian  $H_{\text{ex}}^0$  can be diagonalized using the wave vector representation with corresponding delocalized Bloch states  $\alpha$  and energies  $E_\alpha$ . Using Fourier transformed excitonic operators  $a_\alpha$ , the Hamiltonian in  $\alpha$ -representation reads

$$H_{\text{ex}}^0 = \sum_{\alpha=1}^N E_\alpha a_\alpha^\dagger a_\alpha. \quad (3)$$

The interaction strengths between the nearest neighbour bacteriochlorophylls inside one subunit and between subunits are almost the same in B850 ring from LH2 complex (see Figure 1 (B) in [5]). That is why such ring can be modeled as homogeneous case. If we consider the nearest neighbour approximation model (only the nearest neighbour transfer matrix elements are nonzero), we have

$$\bar{J}_{mn}^{\text{LH2}} = J_0(\delta_{m,n+1} + \delta_{m,n-1}). \quad (4)$$

In this case the form of operators  $a_\alpha$  is

$$a_\alpha = \sum_{n=1}^N a_n e^{i\alpha n}, \quad \alpha = \frac{2\pi}{N}l, \quad l = 0, \dots, \pm \frac{N}{2}, \quad (5)$$

where  $N = 18$  and the simplest exciton Hamiltonian for B850 ring from LH2 complex in  $\alpha$ -representation is given by Eq. (3) with

$$E_\alpha^{\text{LH2}} = -2J_0 \cos \alpha \quad (6)$$

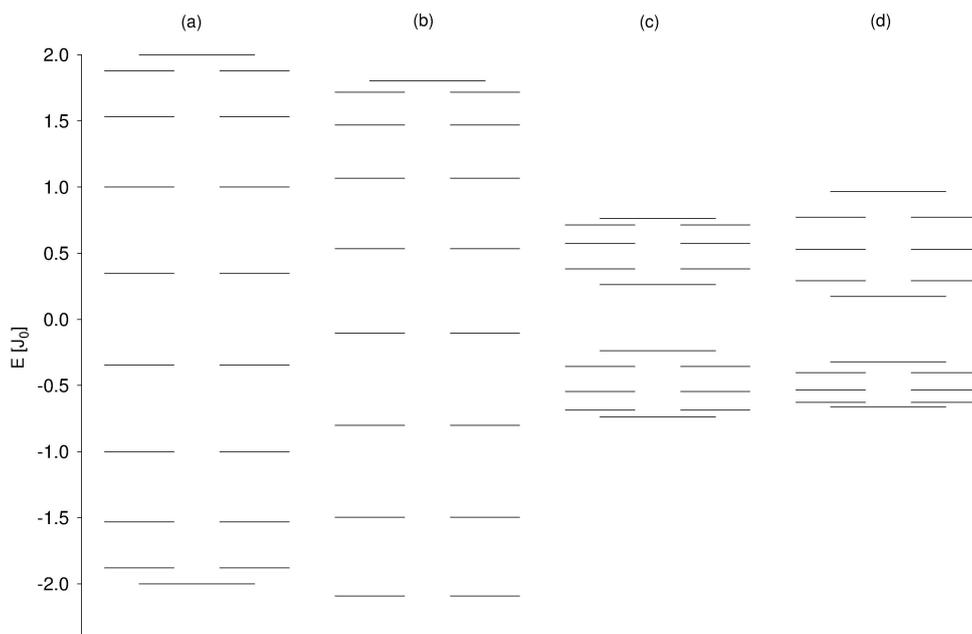


Figure 1: Energetic band structures of B850 ring from LH2 complex ((a) – the nearest neighbour approximation model, (b) – full Hamiltonian model) and the same for B- $\alpha$ /B- $\beta$  ring from LH4 complex ((c) – the nearest neighbour approximation model, (d) – full Hamiltonian model)

(see Figure 1 - column (a)).

B- $\alpha$ /B- $\beta$  ring from LH4 complex consists of 16 BChls ( $N = 16$ ) and it is considerably dimerized - interaction strength between the nearest neighbour bacteriochlorophylls inside one subunit is approximately two times higher in comparison with that between subunits (see Figure 1 (A) in [5]). If the nearest neighbour approximation is taken into account, transfer matrix elements read

$$\bar{J}_{mn}^{\text{LH4}} = -J_0 \left( \frac{\delta_{m,n+1}}{2} + \frac{\delta_{m,n-1}}{4} \right) \quad (7)$$

for odd  $m$  and

$$\bar{J}_{mn}^{\text{LH4}} = -J_0 \left( \frac{\delta_{m,n+1}}{4} + \frac{\delta_{m,n-1}}{2} \right) \quad (8)$$

for even  $m$ . That is why energetic spectrum of B- $\alpha$ /B- $\beta$  ring from LH4 complex is different from that of B850 ring from LH2 complex (see Figure 1 - column (c)).

If we consider full Hamiltonian model in dipole-dipole approximation, transfer integrals  $J_{mn}$  can be written as

$$J_{mn} = \frac{\vec{d}_m \cdot \vec{d}_n}{|\vec{r}_{mn}|^3} - 3 \frac{(\vec{d}_m \cdot \vec{r}_{mn})(\vec{d}_n \cdot \vec{r}_{mn})}{|\vec{r}_{mn}|^5} = |\vec{d}_m||\vec{d}_n| \frac{\cos \varphi_{mn} - 3 \cos \varphi_m \cos \varphi_n}{|\vec{r}_{mn}|^3} \quad (9)$$

Here  $\vec{d}_m$  and  $\vec{d}_n$  are local dipole moments of  $m$ -th and  $n$ -th molecule respectively,  $\vec{r}_{mn}$  is the vector connecting  $m$ -th and  $n$ -th molecule and  $\varphi_m$  ( $\varphi_n$ ) is the angle between  $\vec{d}_m$  ( $\vec{d}_n$ ) and  $\vec{r}_{mn}$ . The angle between  $m$ -th and  $n$ -th vector of local dipole moment ( $\vec{d}_m$ ,  $\vec{d}_n$ ) is referred to as  $\varphi_{mn}$ . In dipole-dipole approximation geometric arrangement of the ring has to correspond with the interaction strengths between the nearest neighbour bacteriochlorophylls. That is why distances  $r_{m,m+1}$  of neighbouring molecules in B850 ring from LH2 complex are the same (without any disorder) and angles  $\beta_{m,m+1}$  have to be the same too ( $\beta_{m,m+1} = 2\pi/18$ , see Figure 2). On the other hand, dimerization is present in B- $\alpha$ /B- $\beta$  ring from

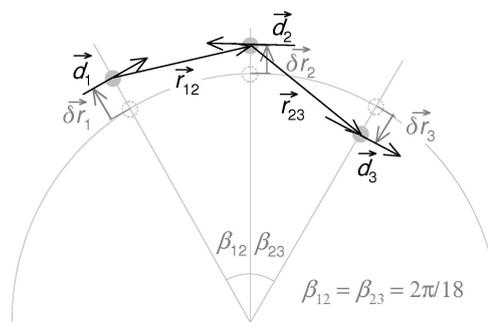


Figure 2: Fluctuations in radial positions of molecules  $\delta r_k$  – B850 ring from LH2 complex

LH4 complex. Therefore the distances  $r_{m,m+1}$  and the angles  $\beta_{m,m+1}$  (see Figure 3) are different and have to correspond to different interaction strengths (see Eq. (7) and Eq. (8)).

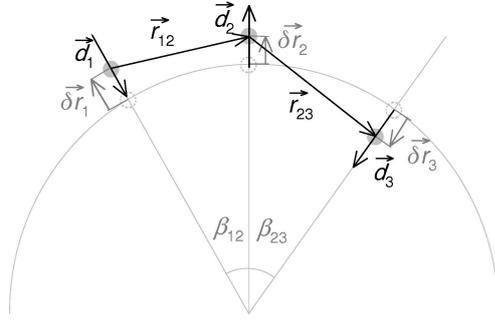


Figure 3: Fluctuations in radial positions of molecules  $\delta r_k$  – B- $\alpha$ /B- $\beta$  ring from LH4 complex

In case of full hamiltonian model energetic band structures slightly differ from that for the nearest neighbour approximation model. For B850 ring from LH2 complex the differences of energies in lower part of the band are higher and in upper part of the band are smaller in comparison with the nearest neighbour approximation model (see Figure 1 - column (b)). On the other hand, differences of the energies in lower part of the band are smaller and in upper part of the band are higher for B- $\alpha$ /B- $\beta$  ring from LH4 complex (see Figure 1 - column (d)).

The second term in Eq. (1),  $H_s$ , corresponds to static disorder. Influence of static disorder is modeled by uncorrelated fluctuations of radial positions of molecules  $\delta r_k$  on the ring (with Gaussian distribution and standard deviation  $\Delta_r$ ),

$$r_k = r_0 + \delta r_k, \quad (10)$$

where  $r_0$  is the radius of the ring without any disorder. Fluctuations  $\delta r_k$  manifest themselves in fluctuations of transfer integrals  $J_{mn}$  but with the distribution different from the Gaussian one [15].

The third term in Eq. (1),

$$H_{\text{ph}} = \sum_q \hbar \omega_q b_q^\dagger b_q, \quad (11)$$

represents phonon bath in harmonic approximation. Phonon creation and annihilation operators are denoted by  $b_q^\dagger$  and  $b_q$ , respectively.

Last term,

$$H_{\text{ex-ph}} = \frac{1}{\sqrt{N}} \sum_m \sum_q G_q^m \hbar \omega_q a_m^\dagger a_m (b_q^\dagger + b_q), \quad (12)$$

describes exciton-phonon interaction which is assumed to be site-diagonal and linear in bath coordinates (the term  $G_q^m$  denotes the exciton-phonon coupling constant).

For the calculation of spectral responses of the system with exciton-phonon coupling we use the cumulant-expansion method of Mukamel et al. [32]. We can express absorption  $OD(\omega)$  and steady-state fluorescence  $FL(\omega)$  spectra as

$$OD(\omega) = \omega \sum_\alpha d_\alpha^2 \times \text{Re} \int_0^\infty dt e^{i(\omega - \omega_\alpha)t - g_{\alpha\alpha\alpha}(t) - R_{\alpha\alpha\alpha}t}, \quad (13)$$

$$FL(\omega) = \omega \sum_\alpha P_\alpha d_\alpha^2 \times \text{Re} \int_0^\infty dt e^{i(\omega - \omega_\alpha)t + i\lambda_{\alpha\alpha\alpha}t - g_{\alpha\alpha\alpha}^*(t) - R_{\alpha\alpha\alpha}t}. \quad (14)$$

Here

$$\vec{d}_\alpha = \sum_n c_n^\alpha \vec{d}_n \quad (15)$$

is the transition dipole moment of the eigenstate  $\alpha$ ,  $c_n^\alpha$  are the expansion coefficients of the eigenstate  $\alpha$  in site representation and  $P_\alpha$  is the steady state population of the eigenstate  $\alpha$ . The inverse lifetime of the exciton state  $\alpha$ ,  $R_{\alpha\alpha\alpha}$ , is given by the elements of Redfield tensor [33] (a sum of the relaxation rates between exciton states)

$$R_{\alpha\alpha\alpha} = - \sum_{\beta \neq \alpha} R_{\beta\beta\alpha}. \quad (16)$$

The g-functions and  $\lambda$ -values in Eq. (14) are given by [32]

$$g_{\alpha\beta\gamma\delta} = - \int_{-\infty}^\infty \frac{d\omega}{2\pi\omega^2} C_{\alpha\beta\gamma\delta}(\omega) \times \left[ \coth \frac{\omega}{2k_B T} (\cos \omega t - 1) - i(\sin \omega t - \omega t) \right], \quad (17)$$

$$\lambda_{\alpha\beta\gamma\delta} = - \lim_{t \rightarrow \infty} \frac{d}{dt} \text{Im} \{ g_{\alpha\beta\gamma\delta}(t) \} = \int_{-\infty}^\infty \frac{d\omega}{2\pi\omega} C_{\alpha\beta\gamma\delta}(\omega). \quad (18)$$

The matrix of the spectral densities  $C_{\alpha\beta\gamma\delta}(\omega)$  in the eigenstate (exciton) representation reflects the coupling of one-exciton states to the manifold of nuclear modes. In what follows, only a diagonal exciton phonon interaction in site representation is used (see Eq. (12)), i.e. only fluctuations of the pigment site energies are assumed and the restriction to the completely uncorrelated dynamical disorder is applied. In such case each site (i.e. each chromophore) has its own bath completely uncoupled from the baths of the

other sites. Furthermore, it is assumed that these independent baths have identical properties

$$C_{mnm'n'}(\omega) = \delta_{mn}\delta_{mm'}\delta_{nn'}C(\omega). \quad (19)$$

After the transformation to exciton representation we have

$$C_{\alpha\beta\gamma\delta}(\omega) = \sum_n c_n^\alpha c_n^\beta c_n^\gamma c_n^\delta C(\omega). \quad (20)$$

Several models of spectral density of the bath are used in literature [34–36]. It is not entirely clear, which model gives the best description of phonon bath in case of ring antenna complexes as LH2 and LH4. In our present investigation we have used the model of Kühn and May [35]

$$C(\omega) = \Theta(\omega)j_0 \frac{\omega^2}{2\omega_c^3} e^{-\omega/\omega_c}, \quad (21)$$

which has its maximum at  $2\omega_c$ .

### 3 Numerical Considerations

To obtain absorption and steady state fluorescence spectra, it is necessary to calculate single ring  $OD(\omega)$  and  $FL(\omega)$  spectra for large number of different static disorder realizations created by random number generator. Finally, these results have to be averaged over all realizations of static disorder.

For our previous calculations of the absorption and steady state fluorescence spectra (with Gaussian uncorrelated static disorder in local excitation energies  $\delta E_n$  and in transfer integrals  $\delta J_{mn}$  taking into account) software package Mathematica [37] was used. Standard numerical integration method used in Mathematica proved to be unsuitable in case of full Hamiltonian model and static disorder  $\delta r_n$  in radial positions of molecules. It was not possible to achieve satisfactory convergence by above mentioned integration method from Mathematica. This is the reason a procedure in Fortran was created for present calculations.

Integrated functions are oscillating and damped (see Eq. (13) and Eq. (14)) and function  $\text{Re } g_{\alpha\alpha\alpha\alpha}(t)$  is non-negative. Therefore absolute values of integrated functions (for individual  $\alpha$ ) satisfy inequalities

$$\left| \text{Re} \left\{ e^{i(\omega-\omega_\alpha)t - g_{\alpha\alpha\alpha\alpha}(t) - R_{\alpha\alpha\alpha\alpha}t} \right\} \right| \leq e^{-R_{\alpha\alpha\alpha\alpha}t}, \quad (22)$$

$$\left| \text{Re} \left\{ e^{i(\omega-\omega_\alpha)t + i\lambda_{\alpha\alpha\alpha\alpha}t - g_{\alpha\alpha\alpha\alpha}^*(t) - R_{\alpha\alpha\alpha\alpha}t} \right\} \right| \leq e^{-R_{\alpha\alpha\alpha\alpha}t}. \quad (23)$$

The whole  $OD(\omega)$  and  $FL(\omega)$  then satisfy

$$OD(\omega) \leq \omega \sum_{\alpha=1}^N d_\alpha^2 \int_0^\infty dt e^{-R_{\alpha\alpha\alpha\alpha}t}, \quad (24)$$

$$FL(\omega) \leq \omega \sum_{\alpha=1}^N P_\alpha d_\alpha^2 \int_0^\infty dt e^{-R_{\alpha\alpha\alpha\alpha}t} \leq \omega \sum_{\alpha=1}^N d_\alpha^2 \int_0^\infty dt e^{-R_{\alpha\alpha\alpha\alpha}t}. \quad (25)$$

Predetermined accuracy could be achieved by integration over finite time interval  $t \in \langle 0, t_0 \rangle$  (instead of  $\langle 0, \infty \rangle$ ). If

$$t_0 \geq \max \{t_\alpha\}, \quad \alpha = 1, \dots, N, \quad (26)$$

where  $t_\alpha$  satisfy condition

$$d_\alpha^2 \left[ \int_0^\infty dt e^{-R_{\alpha\alpha\alpha\alpha}t} - \int_0^{t_\alpha} dt e^{-R_{\alpha\alpha\alpha\alpha}t} \right] = d_\alpha^2 \frac{e^{-R_{\alpha\alpha\alpha\alpha}t_\alpha}}{R_{\alpha\alpha\alpha\alpha}} \leq \frac{Q}{N\omega}, \quad (27)$$

i.e.

$$t_\alpha \geq \frac{1}{R_{\alpha\alpha\alpha\alpha}} \ln \left( \frac{N\omega d_\alpha^2}{QR_{\alpha\alpha\alpha\alpha}} \right), \quad (28)$$

then deviations of  $OD(\omega)$  and  $FL(\omega)$  from precise values are not larger than  $Q$ . Here  $Q$  is arbitrary real positive number and  $N = 18$  for B850 ring from the LH2 complex or  $N = 16$  for B- $\alpha$ /B- $\beta$  ring from the LH4 complex.  $OD(\omega)$  and  $FL(\omega)$  are therefore integrated as sums of contributions from individual cycles of oscillation. These contributions are added until upper limit of integration exceeds  $t_0$ .

### 4 Units and Parameters

Dimensionless energies normalized to the transfer integral  $\bar{J}_{1,2}^{LH2} = J_0$  in B850 ring from the LH2 complex (see Eq. (4)) have been used in our simulations. Estimation of  $J_0$  varies in literature between  $250 \text{ cm}^{-1}$  and  $400 \text{ cm}^{-1}$ . The nearest neighbour transfer integrals in B- $\alpha$ /B- $\beta$  ring (LH4) have opposite sign in comparison with those in B850 ring (LH2). Furthermore, dimerization can be found in LH4 complex in contrast with LH2 complex [5]. That is why the transfer integrals in B- $\alpha$ /B- $\beta$  ring (LH4) differ from those in B850 ring (LH2) also in their absolute values (see Eq. (7) and Eq. (8)). Therefore we have taken the values of the nearest neighbour transfer integrals in B- $\alpha$ /B- $\beta$  ring from the LH4 complex as follows:

$$\bar{J}_{12}^{LH4} = -0.5\bar{J}_{12}^{LH2} = -0.5J_0,$$

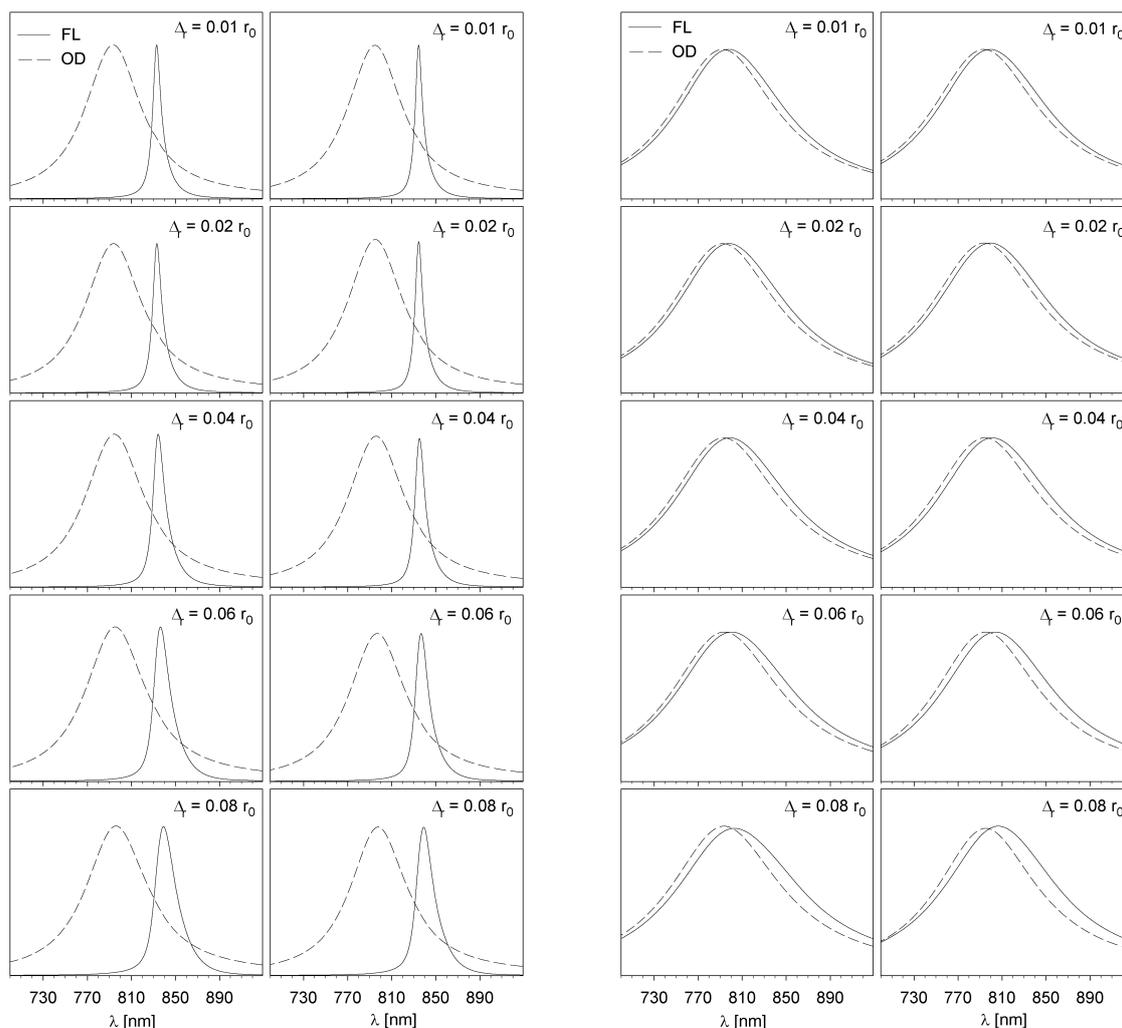


Figure 4: Calculated  $FL(\omega)$  and  $OD(\omega)$  spectra of B- $\alpha$ /B- $\beta$  ring from LH4 complex averaged over 2000 realizations of Gaussian uncorrelated static disorder in radial positions of molecules  $\delta r_k$  (five strengths  $\Delta_r$ , low temperature  $kT = 0.1 J_0$  – first and second column, room temperature  $kT = 0.5 J_0$  – third and fourth column). Full Hamiltonian model – first and third column, the nearest neighbour approximation model – second and fourth column.

$$\bar{J}_{23}^{LH4} = 0.5 \bar{J}_{12}^{LH4} = -0.25 J_0.$$

In our previous investigations [38] we found from comparison with experimental results for B850 ring from the LH2 complex [39] that the possible strength  $\Delta_r$  of the uncorrelated static disorder in radial positions of molecules  $\delta_r$  is approximately  $\Delta_r \approx 0.06 r_0$ . That is why we have taken the strengths  $\Delta_r = 0.01, 0.02, 0.04, 0.06, 0.08 r_0$ . In case of fluctuations in transfer integrals  $\delta J_{mn}$  we suppose that the strength of static disorder is proportional to absolute value of respective transfer integral  $\bar{J}_{mn}$  in the ideal ring (without any disorder)

$$J_{mn} = \bar{J}_{mn} \left( 1 + \frac{\delta J_{mn}}{\bar{J}_{mn}} \right). \quad (29)$$

We have taken the strength of static disorder

$$\Delta_J = 0.225, 0.250, 0.275, 0.300, 0.325 \bar{J}_{mn}.$$

For the best reproduction of experimental data for the LH2 complex [34] within the nearest neighbour approximation model and static disorder in radial positions of molecules on the ring, our previous investigations give the following values of interpigment interaction energy  $J_0$  and unperturbed transition energy from the ground state  $E_0$ :

$$J_0 = 400 \text{ cm}^{-1}, \quad E_0 = 12350 \text{ cm}^{-1}.$$

In order to compare the results for both models of Hamiltonian, we have done the simulations for full Hamiltonian model with the same values  $J_0$  and  $E_0$ . As concerns the spectral density function  $C(\omega)$ , we have used the model of Kühn and May [35] (see Eq.

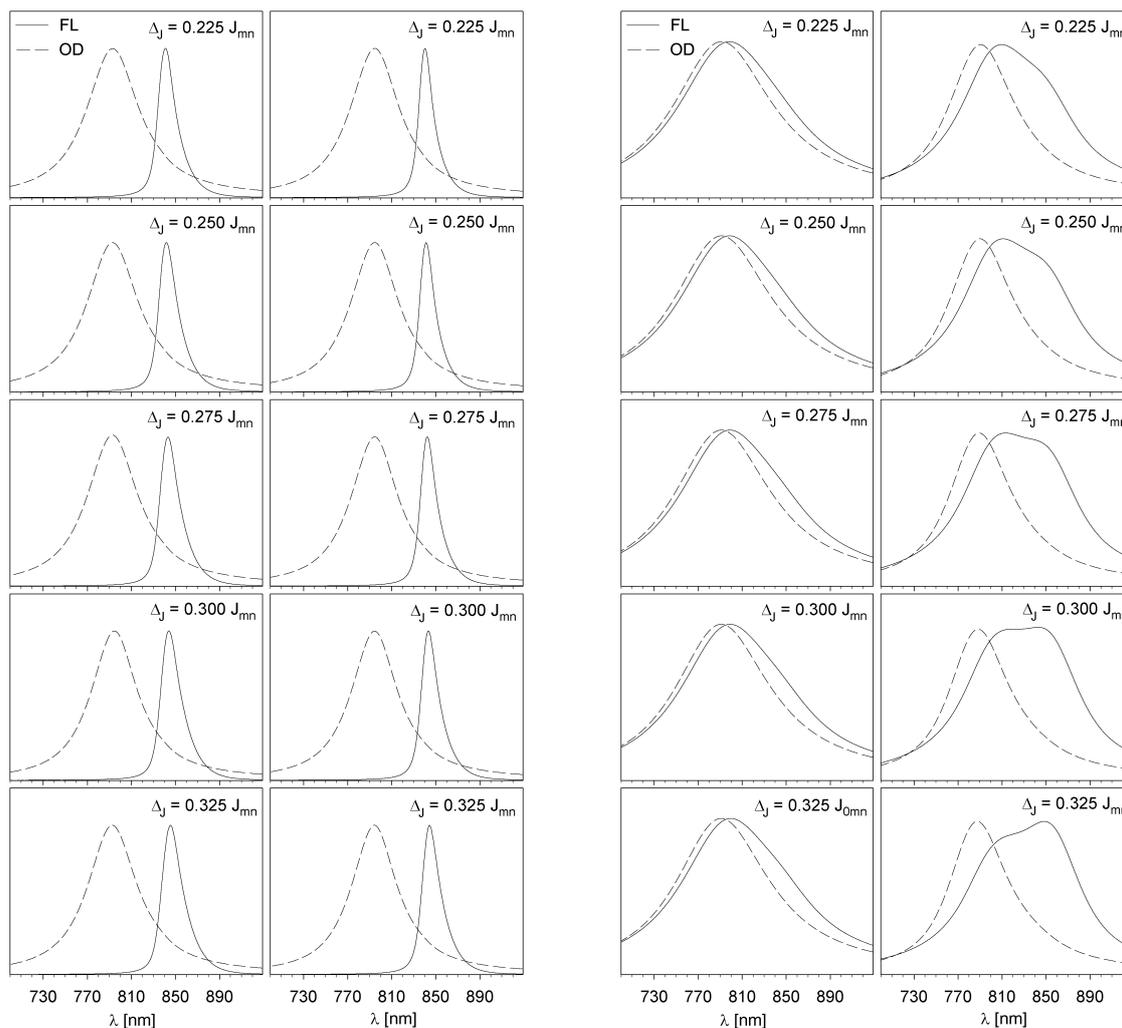


Figure 5: Calculated  $FL(\omega)$  and  $OD(\omega)$  spectra of B- $\alpha$ /B- $\beta$  ring from LH4 complex averaged over 2000 realizations of Gaussian uncorrelated static disorder in transfer integrals  $\delta J_{mn}$  (five strengths  $\Delta_J$ , low temperature  $kT = 0.1 J_0$  – first and second column, room temperature  $kT = 0.5 J_0$  – third and fourth column). Full Hamiltonian model – first and third column, the nearest neighbour approximation model – second and fourth column.

(21)) with values of the parameters  $j_0$  and  $\omega_c$  chosen in agreement with our previous results [16]:

$$j_0 = 0.4J_0, \quad \omega_c = 0.212J_0.$$

## 5 Results and Discussion

Novoderezhkin et al. studied the LH2 complex [34] but only for room temperature and for one type of uncorrelated static disorder (fluctuations of local excitation energies). We did similar calculations for B850 ring from the LH2 complex with the same type of static disorder (fluctuations of local excitation energies) as for the nearest neighbour approximation model (NN) as for full Hamiltonian model (FH) but also for low temperature [22, 26]. Besides this type of static disorder we also used other types of static

disorder (uncorrelated fluctuations  $\delta J_{mn}$  of transfer integrals and uncorrelated fluctuations  $\delta r_m$  of radial positions of molecules on the ring [22, 28]). In addition, the spectral density function  $C(\omega)$  (see Eq. (21)) which differs from that one used by Novoderezhkin et al. [34] was taken into account in our simulations. Previous results for the LH4 complex were published e.g. by Ruijter et al. [5] (fluorescence spectrum) and Read et al. [40] (absorption spectrum) for low temperature. Again we did calculations for NN model as for low temperature as for room temperature and for three above mentioned types of static disorder [23, 24, 29]. The results for FH model and fluctuations in local excitation energies  $\delta \varepsilon_n$  and transfer integrals  $\delta J_{mn}$  were published in [27, 41]. New results for B- $\alpha$ /B- $\beta$  ring from the LH4 complex within FH model and Gaussian uncorrelated static disorder  $\delta r_k$  in radial positions of

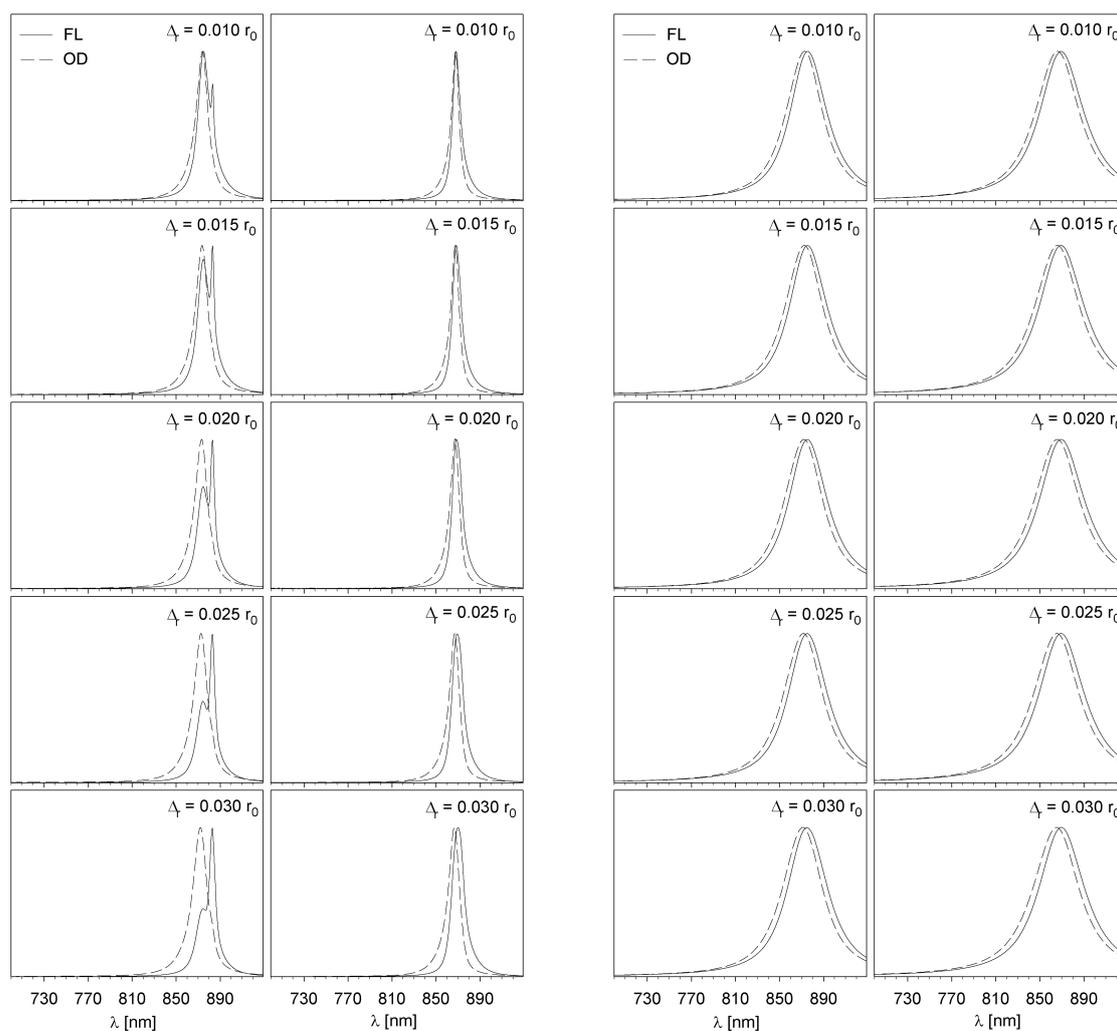


Figure 6: Calculated  $FL(\omega)$  and  $OD(\omega)$  spectra of B850 ring from LH2 complex averaged over 2000 realizations of Gaussian uncorrelated static disorder in radial positions of molecules  $\delta r_k$  (five strengths  $\Delta_r$ , low temperature  $kT = 0.1 J_0$  – first and second column, room temperature  $kT = 0.5 J_0$  – third and fourth column). Full Hamiltonian model – first and third column, the nearest neighbour approximation model – second and fourth column.

molecules on the ring are presented in this paper. Also comparison with our previous results from different viewpoints is done.

Absorption spectra  $OD(\omega)$  and steady state fluorescence spectra  $FL(\omega)$  of B- $\alpha$ /B- $\beta$  ring from the LH4 complex averaged over 2000 realizations of Gaussian uncorrelated static disorder  $\delta r_k$  in radial positions of molecules on the ring can be seen in Figure 4 (first and second column – low temperature  $kT = 0.1 J_0$ , third and fourth column – room temperature  $kT = 0.5 J_0$ ). The same, but for uncorrelated Gaussian static disorder in transfer integrals  $\delta J_{mn}$ , is drawn in Figure 5. Absorption and steady state fluorescence spectra ( $OD(\omega)$  and  $FL(\omega)$ ) of B850 ring from the LH2 complex with the same type of static disorder (fluctuations  $\delta r_k$  in radial positions of molecules on the ring) are shown in Fig-

ure 6 (again first and second column – low temperature  $kT = 0.1 J_0$ , third and fourth column – room temperature  $kT = 0.5 J_0$ ).

At low temperature ( $kT = 0.1 J_0$ ) the steady state fluorescence spectra  $FL(\omega)$  of B850 ring from the LH2 complex substantially differ for FH model and for NN one. Fluorescence spectral line splitting is visible in FH model contrary to NN model. These differences are visible for all three types of static disorder: fluctuations in radial positions of molecules  $\delta r_n$  (Figure 6 – first and second column), fluctuations in local excitation energies  $\delta \epsilon_n$  [26], fluctuations in transfer integrals  $\delta J_{mn}$  [28]. Fluorescence spectra for FH model and for NN one are qualitatively same at room temperature  $kT = 0.5 J_0$  – only one peak appears.

The situation is different in case of B- $\alpha$ /B- $\beta$  ring

from the LH4 complex. The indication of fluorescence spectral line splitting is visible for NN model (contrary to FH model in LH2), but only for room temperature  $kT = 0.5 J_0$ . These differences are visible only for static disorder in transfer integrals  $\delta J_{mn}$  (Figure 5 - third and fourth column) and for static disorder in local excitation energies  $\delta \varepsilon_n$  [27]. In case of fluctuations in radial positions  $\delta r_n$  of molecules, the fluorescence spectrum  $FL(\omega)$  has only one peak for both models of Hamiltonian (NN and FH), as for low temperature  $kT = 0.1 J_0$  as for room one  $kT = 0.5 J_0$  (see Figure (4)).

As concerns absorption spectra  $OD(\omega)$ , both models of Hamiltonian and all types of static disorder give substantially the same results. Only comparison of  $OD(\omega)$  spectra for low and room temperature brings significant difference in spectral width. Absorption spectra are substantially wider for room temperature in comparison with low temperature.

## 6 Conclusions

Comparison of the results obtained within different models of Hamiltonian and different types of static disorder can be summarized as follows. The most essential difference, spectral line splitting, appears in fluorescence spectra. This effect has different reasons for different types of LH complexes. In case of B850 ring from the LH2 complex the splitting is caused by the substitution of NN Hamiltonian model by FH one, but the splitting is not significantly influenced by changing of static disorder type. On the other hand, fluorescence spectral line splitting depends mainly on static disorder type for B- $\alpha$ /B- $\beta$  ring from the LH4 complex. The appearance of this effect is not substantially affected by the model of Hamiltonian in this case. These differences lie in different energetic band structures and different optically active states of these photosynthetic complexes.

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