# Performance comparison of location of optimum TMD on seismic structures 

SİNAN MELİH NİGDELİ<br>Department of Civil Engineering<br>Istanbul University - Cerrahpaşa<br>34320 Avcılar, Faculty of Engineering, Istanbul, Turkey<br>TURKEY<br>melihnig@istanbul.edu.tr<br>GEBRAİL BEKDAS<br>Department of Civil Engineering<br>Istanbul University - Cerrahpaşa<br>34320 Avcilar, Faculty of Engineering, Istanbul, Turkey<br>TURKEY<br>bekdas@istanbul.edu.tr


#### Abstract

The parameters of mechanical components of tuned mass dampers (TMDs) need to optimally tuned for an effective vibration reduction of seismic structures. Generally, metaheuristic algorithms are employed for this optimization problem. In the present study, location of a TMD on a seismic structure is investigated. The case structure is a 15 -story building and the lowest story has a low stiffness to represent a base isolation level. The optimum TMD parameters are found for the placement of TMD on the top and base isolation level. The performance of TMD is best when it is on the top, but the optimum damping ratio value is small for a TMD positioned on the base isolation floor. The optimum TMDs are effective to reduce base isolation floor displacement and structural accelerations.


Key-Words: Tuned Mass Dampers, Structural Control, Optimization, Metaheuristic algorithms, Flower Pollination Algorithms.

## 1 Introduction

The vibrations of civil structures can be reduced by using control systems. These control systems may be passive, active, semi-active or hybrid. Generally, passive systems are less effective in vibration control, but it is more feasible comparing to active control systems which need the generation of a control force by using an external source like linear actuators.
The key factor in a passive control system is the fine tuning. Otherwise, the passive control system may not be effective or it also may be harmful to the structure. Due to this reason, optimization is essential in the design of passive control systems for seismic structures. The optimized values are generally properties of the mechanical components of the system and the main objective is to reduce a critical response of the structure.

Tuned mass dampers and base isolation systems are the examples of passive control systems used in seismic structures. Especially, base isolation systems are effective in reduction of structural accelerations, but the displacement of base isolation level must be kept in a feasible limit to prevent rupture of the rubber isolator systems or to provide a feasible seismic gap around the structure. Nigdeli et al. [1] proposed an optimization methodology to find the optimum period and damping of base isolation systems. A music inspired metaheuristic algorithm called harmony search (HS) [2] was employed in that study. Then, Bekdaş et al. [3] employed Bat algorithm developed by Yang [4] for the same problem.
Tuned mass dampers (TMDs) can be used on all types of mechanical systems including civil structures. The main idea is to tune the frequency (or period) of mass damper close to the first natural frequency (or period) of the structure. In
documented methods, several formulations are proposed for optimum ratio of frequencies ( $\mathrm{f}_{\text {opt }}$ ) of TMD ( $\omega_{\mathrm{d}, \text { opt }}$ ) and superstructure ( $\omega_{\mathrm{s}}$ ) was proposed with the optimum damping ratio $\left(\xi_{\mathrm{d} \text {,opt }}\right)$. Some of the formulations are presented in Table 1. In these formulations, $\mu$ is the ratio of mass of TMD $\left(m_{d}\right)$ and structure (m). The damping coefficient of TMD is shown with $\mathrm{C}_{\mathrm{d} \text {,opt }}$ and $\xi$ is the superstructure damping.
The formulations presented in Table 1 are for single degree of freedom (SDOF) superstructures. These formulations can be used for multiple degree of freedom system by considering a single vibration mode only. For a more general optimum tuning by
considering multiple modes and effect of earthquake excitations, metaheuristic algorithms can be employed [5-22].
In the present study, the position factor of TMD was investigated by positioning TMD on the first and top story of the structure. The case structure is a base isolated building with a soft first story (base isolation level). The optimum TMD parameters are found by using Flower Pollination Algorithm (FPA) developed by Yang [26] and the optimization objective is to reduce the maximum inter story drifts which occur at the base isolation level.

TABLE I. THE FREQUENCY AND DAMPING RATIO EXPRESSIONS OF THE TMD OPTIMIZATION

| Method | $f_{\text {opt }}=\frac{w_{d, \text { opt }}}{w_{s}}$ | $\xi_{d, \text { opt }}=\frac{c_{d, \text { opt }}}{2 m_{d} w_{d, p p t}}$ |
| :--- | :---: | :---: |
| Den Hartog [23] | $\frac{1}{1+\mu}$ | $\sqrt{\frac{3 \mu}{8(1+\mu)}}$ |
| Warburton [24] | $\frac{\sqrt{1-(\mu / 2)}}{1+\mu}$ | $\sqrt{\frac{\mu(1-\mu / 4)}{4(1+\mu)(1-\mu / 2)}}$ |
| Sadek et al. [25] | $\frac{1}{1+\mu}\left[1-\xi \sqrt{\frac{\mu}{1+\mu}}\right]$ | $\frac{\xi}{1+\mu}+\sqrt{\frac{\mu}{1+\mu}}$ |
| Leung \& Zhang <br> [11] | $\frac{\sqrt{1-(\mu / 2)}}{1+\mu}$ | $\sqrt{\frac{\mu(1-\mu / 4)}{4(1+\mu)(1-\mu / 2)}}$ |

## 2 Methodology

In this section, the equations of motion of shear buildings with TMD on the top (Figure 1) and on the first story (Figure 2) are given. The equation of a N-story shear building can be written as Eq. (1) in matrix form.

$$
\begin{equation*}
M \ddot{\mathrm{x}}(\mathrm{t})+C \dot{\mathrm{x}}(\mathrm{t})+K \mathrm{x}(\mathrm{t})=-M\{1\} \ddot{\mathrm{x}}_{\mathrm{g}}(\mathrm{t}) \tag{1}
\end{equation*}
$$

If the TMD is on the top or on the first story (base isolation floor), the mass matrix (M) can be written as follows:
$M=\operatorname{diag}\left[m_{1} m_{2} \ldots \ldots \ldots . . m_{N} m_{d}\right]$
$\ddot{\mathrm{x}}(\mathrm{t}), \dot{\mathrm{x}}(\mathrm{t})$ and $\mathrm{x}(\mathrm{t})$ represent the acceleration, velocity and displacement vectors with respect to
ground and the displacement vector as shown below.
$x(t)=\operatorname{diag}\left[\begin{array}{lllll}x_{1} & x_{2} & \ldots \ldots \ldots x_{N} & x_{d}\end{array}\right]^{\mathrm{T}}$

The stiffness (K) and damping (C) matrices for TMD at the top is as follows:

$C=\left[\begin{array}{ccccccc}\left(c_{1}+c_{2}\right) & -c_{2} & & & & & \\ -c_{2} & \left(c_{2}+c_{3}\right) & -c_{3} & & & & \\ & \cdot & \cdot & & & & \\ & \cdot & \cdot & \cdot & & & \\ & & \cdot & \cdot & \cdot & & \\ & & & & -c_{N} & \left(c_{N}+c_{d}\right) & -c_{d} \\ & & & & & -c_{d} & c_{d}\end{array}\right]$
If the TMD is on the first story, the K and C matrices are written as Eqs. (6) and (7), respectively.

$$
K=\left[\begin{array}{cccccc}
\left(k_{1}+k_{2}+k_{d}\right) & -k_{2} & & & & -k_{d}  \tag{6}\\
-k_{2} & \left(k_{2}+k_{3}\right) & -k_{3} & & & \\
& \cdot & \cdot & & & \\
& \cdot & \cdot & \cdot & & \\
& & \cdot & \cdot & \cdot & \\
& & & -k_{N} & \left(k_{\mathrm{N}}\right) & 0 \\
-k_{d} & \cdot & \cdot & \cdot & \cdot & 0
\end{array}\right)
$$



Figure 1 Model of N -story shear building including a TMD on the top.
m , k and c values are the mass, stiffness and damping coefficient values of a story and lower indices represent the story number or the TMD with d. The period $\left(\mathrm{T}_{\mathrm{d}}\right)$ and damping ratio $\left(\xi_{\mathrm{d}}\right)$ of TMD can be found as follows:
$T_{d}=2 \pi \sqrt{\frac{m_{d}}{k_{d}}}$
$\xi_{d}=2 c_{d} m_{d} \sqrt{\frac{k_{d}}{m_{d}}}$


Figure 2 Model of N-story shear building including a TMD on the first story.

The optimization objective $(\mathrm{f}(\mathrm{x})$ ) is to minimize the maximum inter-story drifts as formulated as Eq. (10) by considering a normalized TMD stroke constraint shown as Eq. (11). st-max is the allowed value for the normalized stroke. The maximum drift of the base isolated structure is always at the first story.

$$
\begin{align*}
& \mathrm{f}(\mathrm{x})=\max \left[\mathrm{x}_{1}\right]  \tag{10}\\
& \frac{\max \left[\left|\mathrm{x}_{\mathrm{d}}-\mathrm{x}_{\mathrm{N}}\right|\right]_{\text {with TMD }}}{\max \left[\left|\mathrm{x}_{\mathrm{N}}\right| \|_{\text {without TMD }}\right.} \leq \mathrm{st}_{-} \max \tag{11}
\end{align*}
$$

The mass of the structure is taken as constant. $\mathrm{T}_{\mathrm{d}}$ and $\xi_{d}$ are the design variables searched for a set of earthquake records (Table II) by using Flower Pollination Algorithm (FPA).

In nature, flowers reproduce by pollination in two ways. In the first way, pollens can be transferred by pollinators such as insects, birds, bats or other animals (cross-pollination). In the second way, some flower types have ability for self-pollination. According to the following four rules, FPA is developed [26].
1.The pollinators obey the rules of a Lévy distribution in cross-pollination and it is the global pollination process.
2.Self-pollination is local pollination process and it occurs from pollen of the same flower species.
3.Flower constancy is used as a reproduction strategy. İt is the similarity of two flowers involved in pollination.
4.A probability is used to choose the pollination type. It is called the switch probability.
In the optimization methodology, design constants (structural properties, external excitations and ranges of design variables) are initially defined. Then, the super-structure (the building without TMD) is analyzed. Then, the results will be used to compare the effectiveness of the TMD. Then, the initial solutions for design variables such as period and damping ratio of TMD are randomly generated and the dynamic analyses are done for all set of variables as many as population number. Then, the iterative optimization process starts.

TABLE II. FEMA FAR-FAULT RECORDS [27]

| Earthquake No. | Earthquake Name | Recording Station | Year | Magnitude | FN Component | FP Component |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Northridge | Beverly Hills Mulhol | 1994 | 6,7 | NORTHR/MUL009 | NORTHR/MUL279 |
| 2 | Northridge | Canyon Country-WLC | 1994 | 6,7 | NORTHR/LOS000 | NORTHR/LOS270 |
| 3 | Duzce, Turkey | Bolu | 1999 | 7,1 | DUZCE/BOL000 | DUZCE/BOL090 |
| 4 | Hector Mine | Hector | 1999 | 7,1 | HECTOR/HEC000 | HECTOR/HEC090 |
| 5 | Imperial <br> Valley | Delta | 1979 | 6,5 | IMPVALL/H-DLT262 | $\begin{aligned} & \text { IMPVALL/H- } \\ & \text { DLT352 } \end{aligned}$ |
| 6 | Imperial Valley | El Centro Array \#11 | 1979 | 6,5 | IMPVALL/H-E11140 | IMPVALL/H-E11230 |
| 7 | Kobe, Japan | Nishi-Akashi | 1995 | 6,9 | KOBE/NIS000 | KOBE/NIS090 |
| 8 | Kobe, Japan | Shin-Osaka | 1995 | 6,9 | KOBE/SHI000 | KOBE/SHI090 |
| 9 | Kocaeli, Turkey | Duzce | 1999 | 7,5 | KOCAELI/DZC180 | KOCAELI/DZC270 |
| 10 | Kocaeli, Turkey | Arcelik | 1999 | 7,5 | KOCAELI/ARC000 | KOCAELI/ARC090 |
| 11 | Landers | Yermo Fire Station | 1992 | 7,3 | LANDERS/YER270 | LANDERS/YER360 |
| 12 | Landers | Coolwater | 1992 | 7,3 | LANDERS/CLW-LN | LANDERS/CLW-TR |
| 13 | Loma Prieta | Capitola | 1989 | 6,9 | LOMAP/CAP000 | LOMAP/CAP090 |
| 14 | Loma Prieta | Gilroy Array \#3 | 1989 | 6,9 | LOMAP/G03000 | LOMAP/G03090 |
| 15 | Manjil, Iran | Abbar | 1990 | 7.4 | MANJIL/ABBAR--L | MANJIL/ABBAR--T |
| 16 | Superstition Hills | El Centro Imp. Co. | 1987 | 6.5 | SUPERST/B-ICC000 | SUPERST/B-ICC090 |
| 17 | Superstition Hills | Poe Road (temp) | 1987 | 6.5 | SUPERST/B-POE270 | SUPERST/B-POE360 |
| 18 | Cape <br> Mendocino | Rio Dell <br> Overpass  | 1992 | 7.0 | CAPEMEND/RIO270 | CAPEMEND/RIO360 |
| 19 | Chi-Chi, <br> Taiwan | CHY101 | 1999 | 7.6 | CHICHI/CHY101-E | CHICHI/CHY101-N |
| 20 | Chi-Chi, Taiwan | TCU045 | 1999 | 7.6 | CHICHI/TCU045-E | CHICHI/TCU045-N |
| 21 | San Fernando | LA Hollywood Stor | 1971 | 6.6 | SFERN/PEL090 | SFERN/PEL180 |
| 22 | Friuli, Italy | Tolmezzo | 1976 | 6.5 | FRIULI/A-TMZ000 | FRIULI/A-TMZ270 |

In the global pollination, the solution of the next step $\left(\mathrm{x}_{\mathrm{i}}^{(+1}\right)$ is found by using the values of the previous step (step $t$ ) defined as $x_{i}^{t}$ (Eq. (12)).
$\mathrm{x}_{\mathrm{i}}^{\mathrm{t}+1}=\mathrm{xi}_{\mathrm{i}}^{\mathrm{t}}+\mathrm{L}\left(\mathrm{x}_{\mathrm{i}}^{\mathrm{t}}-\mathrm{g} *\right)$
In Eq. (12), i represents the $i$-th pollen, $\mathrm{g}_{*}$ is the current best solution and L is a Lévy distribution.
Local pollination is formulized with random walks as seen in Eq. (13).
$\mathrm{x}_{\mathrm{i}}^{\mathrm{t}+1}=\mathrm{x}_{\mathrm{i}}^{\mathrm{t}}+\in\left(\mathrm{x}_{\mathrm{j}}{ }^{\mathrm{t}}-\mathrm{x}_{\mathrm{k}}{ }^{\mathrm{t}}\right)$
In local pollination, $\mathrm{x}_{\mathrm{j}}{ }^{\mathrm{t}}$ and $\mathrm{x}_{\mathrm{k}}{ }^{\mathrm{t}}$ are solution of different plants. $\in$ is a linear distribution randomized between 0 and 1 . The iteration continue until the objective function is minimized.

## 3 Numerical Example

The properties of the structure model are given as Table III. The maximum drift and acceleration of the structure under FEMA far-field earthquake records as given in Tables IV and V, respectively. The maximum responses occur for the fault parallel component of $19^{\text {th }}$ station. The maximum displacement of the first story is 1.271 m and the maximum acceleration is $6.7262 \mathrm{~m} / \mathrm{s}^{2}$.

TABLE III. Properties of Structure [28]

| Story | Mass | Stiffness | Damping <br> Coefficient |
| :--- | :--- | :--- | :--- |
| 1 | $4.500 \times 10^{5}$ | $1.805 \times 10^{7}$ | $2.617 \times 10^{4}$ |
| $2-15$ | $3.456 \times 10^{5}$ | $3.404 \times 10^{8}$ | $2.937 \times 10^{5}$ |

TABLE IV. The MAximum Drift of Structure

| EQ/i | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1,FN | 0.190 | 0.008 | 0.010 | 0.012 | 0.014 | 0.015 | 0.017 | 0.017 | 0.017 | 0.017 | 0.015 | 0.013 | 0.010 | 0.007 | 0.004 |
| 1,FP | 0.160 | 0.007 | 0.008 | 0.009 | 0.010 | 0.011 | 0.012 | 0.012 | 0.012 | 0.011 | 0.010 | 0.009 | 0.007 | 0.005 | 0.002 |
| 2,FN | 0.171 | 0.009 | 0.009 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.007 | 0.006 | 0.005 | 0.004 | 0.004 | 0.003 | 0.001 |
| 2,FP | 0.189 | 0.009 | 0.009 | 0.010 | 0.010 | 0.010 | 0.009 | 0.009 | 0.009 | 0.008 | 0.007 | 0.006 | 0.005 | 0.003 | 0.002 |
| 3,FN | 0.350 | 0.016 | 0.016 | 0.017 | 0.016 | 0.016 | 0.016 | 0.016 | 0.015 | 0.013 | 0.012 | 0.011 | 0.009 | 0.006 | 0.003 |
| 3,FP | 0.202 | 0.010 | 0.010 | 0.010 | 0.010 | 0.011 | 0.013 | 0.013 | 0.014 | 0.013 | 0.012 | 0.010 | 0.008 | 0.005 | 0.003 |
| 4,FN | 0.163 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.007 | 0.007 | 0.006 | 0.006 | 0.005 | 0.004 | 0.002 | 0.001 |
| 4,FP | 0.212 | 0.011 | 0.011 | 0.010 | 0.010 | 0.009 | 0.008 | 0.008 | 0.007 | 0.007 | 0.006 | 0.006 | 0.005 | 0.004 | 0.002 |
| 5,FN | 0.468 | 0.022 | 0.020 | 0.019 | 0.018 | 0.017 | 0.016 | 0.015 | 0.013 | 0.012 | 0.010 | 0.009 | 0.007 | 0.005 | 0.002 |
| 5,FP | 0.241 | 0.012 | 0.013 | 0.014 | 0.014 | 0.014 | 0.014 | 0.013 | 0.013 | 0.011 | 0.010 | 0.008 | 0.006 | 0.004 | 0.002 |
| 6,FN | 0.306 | 0.015 | 0.014 | 0.013 | 0.013 | 0.012 | 0.011 | 0.011 | 0.010 | 0.009 | 0.008 | 0.007 | 0.005 | 0.004 | 0.002 |
| 6,FP | 0.235 | 0.011 | 0.011 | 0.010 | 0.010 | 0.010 | 0.009 | 0.008 | 0.007 | 0.006 | 0.005 | 0.005 | 0.004 | 0.003 | 0.001 |
| 7,FN | 0.145 | 0.007 | 0.009 | 0.010 | 0.011 | 0.011 | 0.011 | 0.010 | 0.009 | 0.009 | 0.009 | 0.009 | 0.007 | 0.005 | 0.003 |
| 7,FP | 0.162 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.007 | 0.007 | 0.007 | 0.007 | 0.006 | 0.005 | 0.004 | 0.002 |
| 8,FN | 0.180 | 0.009 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.007 | 0.007 | 0.007 | 0.006 | 0.004 | 0.003 | 0.002 |
| 8,FP | 0.139 | 0.007 | 0.006 | 0.007 | 0.007 | 0.007 | 0.007 | 0.006 | 0.006 | 0.005 | 0.004 | 0.004 | 0.003 | 0.002 | 0.001 |
| 9,FN | 1.174 | 0.058 | 0.055 | 0.051 | 0.048 | 0.044 | 0.040 | 0.036 | 0.032 | 0.027 | 0.023 | 0.018 | 0.014 | 0.009 | 0.005 |
| 9,FP | 0.417 | 0.020 | 0.020 | 0.019 | 0.019 | 0.018 | 0.017 | 0.016 | 0.015 | 0.013 | 0.011 | 0.009 | 0.007 | 0.005 | 0.003 |
| 10,FN | 0.111 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.004 | 0.004 | 0.004 | 0.003 | 0.003 | 0.002 | 0.002 | 0.001 | 0.001 |
| 10,FP | 0.332 | 0.016 | 0.015 | 0.015 | 0.014 | 0.013 | 0.012 | 0.011 | 0.010 | 0.009 | 0.007 | 0.006 | 0.005 | 0.003 | 0.002 |
| 11,FN | 0.343 | 0.017 | 0.016 | 0.016 | 0.015 | 0.014 | 0.014 | 0.013 | 0.011 | 0.010 | 0.009 | 0.007 | 0.006 | 0.004 | 0.002 |
| 11,FP | 0.278 | 0.013 | 0.012 | 0.012 | 0.013 | 0.012 | 0.012 | 0.011 | 0.010 | 0.009 | 0.008 | 0.007 | 0.005 | 0.004 | 0.002 |
| 12,FN | 0.139 | 0.006 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.006 | 0.006 | 0.006 | 0.005 | 0.004 | 0.003 | 0.001 |
| 12,FP | 0.107 | 0.005 | 0.005 | 0.005 | 0.006 | 0.005 | 0.005 | 0.004 | 0.004 | 0.005 | 0.005 | 0.004 | 0.004 | 0.003 | 0.001 |
| 13,FN | 0.076 | 0.004 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.004 | 0.003 | 0.002 |
| 13,FP | 0.124 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.005 | 0.005 | 0.004 | 0.003 | 0.002 | 0.001 |
| 14,FN | 0.200 | 0.010 | 0.009 | 0.009 | 0.009 | 0.009 | 0.008 | 0.008 | 0.008 | 0.007 | 0.007 | 0.006 | 0.005 | 0.004 | 0.002 |
| 14,FP | 0.229 | 0.011 | 0.011 | 0.011 | 0.011 | 0.010 | 0.010 | 0.009 | 0.008 | 0.007 | 0.006 | 0.006 | 0.005 | 0.003 | 0.002 |
| 15,FN | 0.334 | 0.016 | 0.015 | 0.014 | 0.013 | 0.013 | 0.012 | 0.011 | 0.010 | 0.009 | 0.008 | 0.006 | 0.005 | 0.004 | 0.002 |
| 15,FP | 0.395 | 0.019 | 0.018 | 0.017 | 0.017 | 0.016 | 0.014 | 0.013 | 0.012 | 0.011 | 0.010 | 0.008 | 0.007 | 0.005 | 0.002 |
| 16,FN | 0.543 | 0.027 | 0.025 | 0.024 | 0.023 | 0.021 | 0.020 | 0.018 | 0.016 | 0.014 | 0.012 | 0.009 | 0.007 | 0.005 | 0.002 |
| 16,FP | 0.339 | 0.017 | 0.016 | 0.015 | 0.014 | 0.013 | 0.012 | 0.011 | 0.010 | 0.009 | 0.007 | 0.006 | 0.005 | 0.003 | 0.002 |
| 17,FN | 0.278 | 0.014 | 0.014 | 0.014 | 0.013 | 0.013 | 0.012 | 0.011 | 0.010 | 0.010 | 0.009 | 0.008 | 0.006 | 0.005 | 0.002 |
| 17,FP | 0.264 | 0.014 | 0.013 | 0.013 | 0.013 | 0.012 | 0.011 | 0.011 | 0.010 | 0.009 | 0.008 | 0.006 | 0.005 | 0.003 | 0.002 |
| 18,FN | 0.127 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.005 | 0.005 | 0.004 | 0.003 | 0.002 | 0.001 |
| 18,FP | 0.098 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.004 | 0.003 | 0.002 |
| 19,FN | 1.154 | 0.057 | 0.054 | 0.051 | 0.049 | 0.046 | 0.043 | 0.039 | 0.035 | 0.031 | 0.027 | 0.022 | 0.017 | 0.011 | 0.006 |
| 19,FP | 1.271 | 0.060 | 0.057 | 0.056 | 0.054 | 0.052 | 0.049 | 0.046 | 0.042 | 0.037 | 0.032 | 0.027 | 0.020 | 0.014 | 0.007 |
| 20,FN | 0.162 | 0.009 | 0.008 | 0.008 | 0.008 | 0.008 | 0.007 | 0.006 | 0.005 | 0.005 | 0.005 | 0.005 | 0.004 | 0.003 | 0.001 |
| 20,FP | 0.148 | 0.007 | 0.007 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.007 | 0.006 | 0.005 | 0.004 | 0.002 |
| 21,FN | 0.420 | 0.020 | 0.019 | 0.019 | 0.018 | 0.016 | 0.015 | 0.014 | 0.013 | 0.012 | 0.010 | 0.008 | 0.006 | 0.004 | 0.002 |
| 21,FP | 0.171 | 0.008 | 0.007 | 0.007 | 0.007 | 0.007 | 0.006 | 0.006 | 0.006 | 0.005 | 0.004 | 0.004 | 0.003 | 0.002 | 0.001 |
| 22,FN | 0.084 | 0.004 | 0.004 | 0.004 | 0.005 | 0.005 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.003 | 0.003 | 0.002 | 0.001 |
| 22,FP | 0.098 | 0.005 | 0.005 | 0.005 | 0.005 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.003 | 0.003 | 0.002 | 0.001 |

TABLE V. The MAximum Acceleration of Structure

| EQ/i | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1,FN | 3.395 | 3.322 | 3.085 | 2.835 | 2.505 | 2.029 | 1.395 | 0.898 | 0.995 | 1.522 | 2.074 | 2.650 | 3.133 | 3.460 | 3.620 |
| 1,FP | 2.395 | 2.331 | 2.206 | 1.961 | 1.769 | 1.601 | 1.414 | 1.442 | 1.226 | 1.179 | 1.468 | 1.793 | 2.096 | 2.334 | 2.447 |
| 2,FN | 1.376 | 1.299 | 1.050 | 0.935 | 1.021 | 1.145 | 1.112 | 1.094 | 1.179 | 1.196 | 1.283 | 1.188 | 1.033 | 1.228 | 1.396 |
| 2,FP | 1.506 | 1.488 | 1.384 | 1.272 | 1.130 | 1.009 | 0.898 | 1.034 | 0.975 | 1.041 | 1.139 | 1.338 | 1.487 | 1.585 | 1.658 |
| 3,FN | 2.717 | 2.567 | 2.433 | 2.654 | 2.705 | 2.548 | 2.174 | 1.743 | 1.860 | 2.053 | 2.303 | 2.316 | 2.587 | 3.068 | 3.324 |
| 3,FP | 2.440 | 2.443 | 2.415 | 2.173 | 1.725 | 1.303 | 1.161 | 0.922 | 1.148 | 1.281 | 1.830 | 2.263 | 2.501 | 2.570 | 2.654 |
| 4,FN | 1.011 | 0.994 | 0.923 | 0.863 | 0.808 | 0.720 | 0.673 | 0.612 | 0.664 | 0.796 | 0.907 | 1.014 | 1.125 | 1.207 | 1.253 |
| 4,FP | 1.629 | 1.563 | 1.366 | 1.094 | 1.159 | 1.296 | 1.373 | 1.389 | 1.407 | 1.282 | 1.081 | 1.038 | 1.373 | 1.664 | 1.825 |
| 5,FN | 1.885 | 1.919 | 1.904 | 1.856 | 1.864 | 1.868 | 1.829 | 1.744 | 1.669 | 1.750 | 1.866 | 1.943 | 2.085 | 2.199 | 2.259 |
| 5,FP | 2.072 | 2.041 | 1.905 | 1.725 | 1.553 | 1.418 | 1.305 | 1.118 | 1.183 | 1.441 | 1.673 | 1.865 | 2.003 | 2.113 | 2.205 |
| 6,FN | 1.632 | 1.561 | 1.426 | 1.379 | 1.380 | 1.333 | 1.259 | 1.262 | 1.293 | 1.297 | 1.342 | 1.425 | 1.613 | 1.758 | 1.839 |
| 6,FP | 1.350 | 1.260 | 1.101 | 1.100 | 1.160 | 1.201 | 1.228 | 1.217 | 1.369 | 1.311 | 1.124 | 1.093 | 1.179 | 1.390 | 1.466 |
| 7,FN | 2.724 | 2.439 | 2.067 | 1.520 | 1.502 | 1.720 | 1.996 | 1.949 | 1.765 | 1.586 | 1.449 | 1.433 | 1.970 | 2.507 | 2.839 |
| 7,FP | 2.041 | 1.842 | 1.474 | 1.056 | 0.952 | 1.049 | 1.165 | 1.223 | 1.198 | 1.075 | 0.959 | 1.021 | 1.390 | 1.787 | 2.038 |
| 8,FN | 1.540 | 1.579 | 1.529 | 1.386 | 1.163 | 0.907 | 0.846 | 0.849 | 0.839 | 0.878 | 0.953 | 1.138 | 1.350 | 1.489 | 1.577 |
| 8,FP | 0.885 | 0.863 | 0.847 | 0.841 | 0.821 | 0.800 | 0.730 | 0.722 | 0.760 | 0.832 | 0.864 | 0.851 | 0.901 | 0.971 | 1.006 |
| 9,FN | 3.422 | 3.574 | 3.704 | 3.815 | 3.906 | 3.980 | 4.056 | 4.162 | 4.272 | 4.365 | 4.441 | 4.498 | 4.536 | 4.557 | 4.575 |
| 9,FP | 1.979 | 2.013 | 1.997 | 1.940 | 1.856 | 1.762 | 1.660 | 1.536 | 1.626 | 1.802 | 1.946 | 2.127 | 2.303 | 2.427 | 2.491 |
| 10,FN | 0.491 | 0.503 | 0.503 | 0.480 | 0.476 | 0.473 | 0.495 | 0.489 | 0.514 | 0.516 | 0.557 | 0.559 | 0.568 | 0.610 | 0.643 |
| 10,FP | 1.168 | 1.202 | 1.227 | 1.250 | 1.256 | 1.250 | 1.232 | 1.202 | 1.195 | 1.263 | 1.325 | 1.385 | 1.444 | 1.497 | 1.526 |
| 11,FN | 1.710 | 1.643 | 1.551 | 1.518 | 1.526 | 1.516 | 1.472 | 1.390 | 1.382 | 1.523 | 1.615 | 1.660 | 1.765 | 1.883 | 1.949 |
| 11,FP | 1.560 | 1.565 | 1.579 | 1.556 | 1.488 | 1.368 | 1.218 | 1.064 | 1.087 | 1.278 | 1.453 | 1.581 | 1.651 | 1.735 | 1.814 |
| 12,FN | 1.349 | 1.285 | 1.162 | 1.104 | 1.102 | 1.005 | 0.874 | 0.759 | 0.770 | 0.841 | 0.952 | 1.000 | 1.142 | 1.281 | 1.458 |
| 12,FP | 1.334 | 1.168 | 0.916 | 0.780 | 0.815 | 0.829 | 0.878 | 0.871 | 0.781 | 0.773 | 0.766 | 0.708 | 0.972 | 1.267 | 1.436 |
| 13,FN | 1.131 | 1.090 | 1.002 | 1.011 | 1.110 | 1.116 | 1.005 | 0.744 | 0.648 | 0.761 | 0.850 | 0.905 | 1.136 | 1.420 | 1.624 |
| 13,FP | 0.889 | 0.876 | 0.840 | 0.778 | 0.870 | 0.887 | 0.852 | 0.768 | 0.849 | 0.927 | 0.906 | 0.876 | 0.986 | 1.038 | 1.063 |
| 14,FN | 1.634 | 1.480 | 1.242 | 1.104 | 1.073 | 1.138 | 1.129 | 1.133 | 1.073 | 1.181 | 1.181 | 1.137 | 1.396 | 1.659 | 1.815 |
| 14,FP | 1.446 | 1.292 | 1.147 | 1.102 | 1.209 | 1.236 | 1.150 | 1.121 | 1.132 | 1.124 | 1.167 | 1.213 | 1.325 | 1.515 | 1.632 |
| 15,FN | 1.495 | 1.322 | 1.481 | 1.494 | 1.363 | 1.432 | 1.484 | 1.339 | 1.325 | 1.425 | 1.572 | 1.602 | 1.539 | 1.701 | 1.878 |
| 15,FP | 1.923 | 1.830 | 1.873 | 1.830 | 1.653 | 1.663 | 1.599 | 1.596 | 1.578 | 1.715 | 1.826 | 1.879 | 2.010 | 2.194 | 2.324 |
| 16,FN | 1.868 | 1.938 | 1.985 | 2.007 | 2.008 | 1.991 | 1.961 | 1.924 | 1.987 | 2.094 | 2.187 | 2.263 | 2.323 | 2.364 | 2.384 |
| 16,FP | 1.146 | 1.183 | 1.207 | 1.211 | 1.224 | 1.303 | 1.362 | 1.378 | 1.344 | 1.277 | 1.296 | 1.388 | 1.474 | 1.548 | 1.589 |
| 17,FN | 1.945 | 1.800 | 1.585 | 1.358 | 1.397 | 1.568 | 1.700 | 1.734 | 1.638 | 1.521 | 1.434 | 1.465 | 1.840 | 2.151 | 2.324 |
| 17,FP | 1.596 | 1.510 | 1.362 | 1.353 | 1.444 | 1.432 | 1.275 | 1.172 | 1.235 | 1.352 | 1.425 | 1.527 | 1.535 | 1.592 | 1.779 |
| 18,FN | 1.030 | 0.974 | 0.950 | 0.946 | 0.958 | 0.784 | 0.633 | 0.600 | 0.565 | 0.812 | 0.932 | 1.020 | 0.956 | 1.072 | 1.172 |
| 18,FP | 1.474 | 1.268 | 0.985 | 0.862 | 1.095 | 1.277 | 1.256 | 1.092 | 1.245 | 1.205 | 1.018 | 0.872 | 1.083 | 1.330 | 1.523 |
| 19,FN | 4.216 | 4.343 | 4.402 | 4.392 | 4.389 | 4.353 | 4.247 | 4.213 | 4.206 | 4.501 | 4.809 | 5.084 | 5.304 | 5.456 | 5.533 |
| 19,FP | 5.552 | 5.754 | 5.881 | 5.907 | 5.812 | 5.590 | 5.247 | 4.807 | 4.721 | 5.203 | 5.661 | 6.092 | 6.458 | 6.726 | 6.869 |
| 20,FN | 1.213 | 1.101 | 0.938 | 0.717 | 0.994 | 1.212 | 1.309 | 1.296 | 1.233 | 1.064 | 0.905 | 0.844 | 1.089 | 1.252 | 1.404 |
| 20,FP | 1.633 | 1.553 | 1.446 | 1.282 | 1.160 | 1.045 | 0.934 | 0.776 | 0.767 | 0.869 | 1.056 | 1.223 | 1.408 | 1.652 | 1.825 |
| 21,FN | 1.751 | 1.783 | 1.771 | 1.724 | 1.675 | 1.695 | 1.691 | 1.649 | 1.675 | 1.755 | 1.789 | 1.890 | 2.041 | 2.151 | 2.208 |
| 21,FP | 0.854 | 0.865 | 0.856 | 0.843 | 0.815 | 0.765 | 0.700 | 0.641 | 0.662 | 0.676 | 0.742 | 0.810 | 0.884 | 0.960 | 1.007 |
| 22,FN | 0.963 | 0.898 | 0.765 | 0.661 | 0.849 | 0.886 | 0.811 | 0.741 | 0.751 | 0.789 | 0.720 | 0.620 | 0.790 | 0.926 | 1.002 |
| 22,FP | 1.002 | 0.856 | 0.631 | 0.547 | 0.654 | 0.803 | 0.941 | 0.926 | 0.884 | 0.804 | 0.660 | 0.636 | 0.762 | 1.015 | 1.150 |

The mass of TMD is taken as $10 \%$ of the total mass of the structure. The stmax is taken as 2 . Also, the design variables are searched in the following ranges:
TMD period: Between 0.5 and 1.5 times of the critical period of the super-structure
TMD damping ratio: Between $1 \%$ and $30 \%$
The optimum TMD parameters are presented in Table VI. According to the results, the positioning of TMD on the top is more effective in the reduction of the objective function. An increase in the period
and the reduction of the damping ratio is seen for the optimum TMD positioned on the base floor.
The critical excitation for the TMD controlled structure are also the same. By using an optimum TMD on the top, it is possible to reduce the base isolation floor displacement to 0.929 m for the critical excitation. This value is also a big one for the rupture protection of base isolators. In that case, additional damping is needed for the base isolation floor. For the TMD on the base floor, the critical displacement reduces to 1 m .

TABLE VI. The Optimum Results

| Story | $\mathrm{m}_{\mathrm{d}}(\mathrm{kg})$ | $\mathrm{T}_{\mathrm{d}}(\mathrm{s})$ | $\xi_{\mathrm{d}}(\mathrm{kg})$ | $\max \left(\mathrm{X}_{1}\right)(\mathrm{m})$ |
| :--- | :--- | :--- | :--- | :--- |
| On the top floor | $5.2884 \times 10^{5}$ | 5.3581 | 0.2433 | 0.929 |
| On the base floor | $5.2884 \times 10^{5}$ | 5.6855 | 0.1715 | 1.00 |

## 4 Conclusions

Generally, additional damping is needed for preventing the maximum displacement of base isolation floors. By the increase of the damping, the performance of base isolation on reduction of structural accelerations reduces. In the present study, the optimum TMDs is effective in reduction of displacement of base isolation floor and additional TMD is also effective to reduce maximum accelerations by $15.2 \%$ and $17.8 \%$ by positioning on the base floor and top, respectively.

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In the case structure, the base floor displacement reduces up to $26.9 \%$, but it is not enough for rupture protection of base isolator and more additional damping is in need. Also, the stroke of TMD limitation may be enlarged for a better performance, but the allowed stroke capacity ( $s t m a x=2$ ) is also a big value. As a conclusion, TMDs are effective to reduce the base displacement of the base isolated structure with an acceleration reduction bonus, but this reduction may not be feasible without additional damping for the base isolation floor.
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